

---

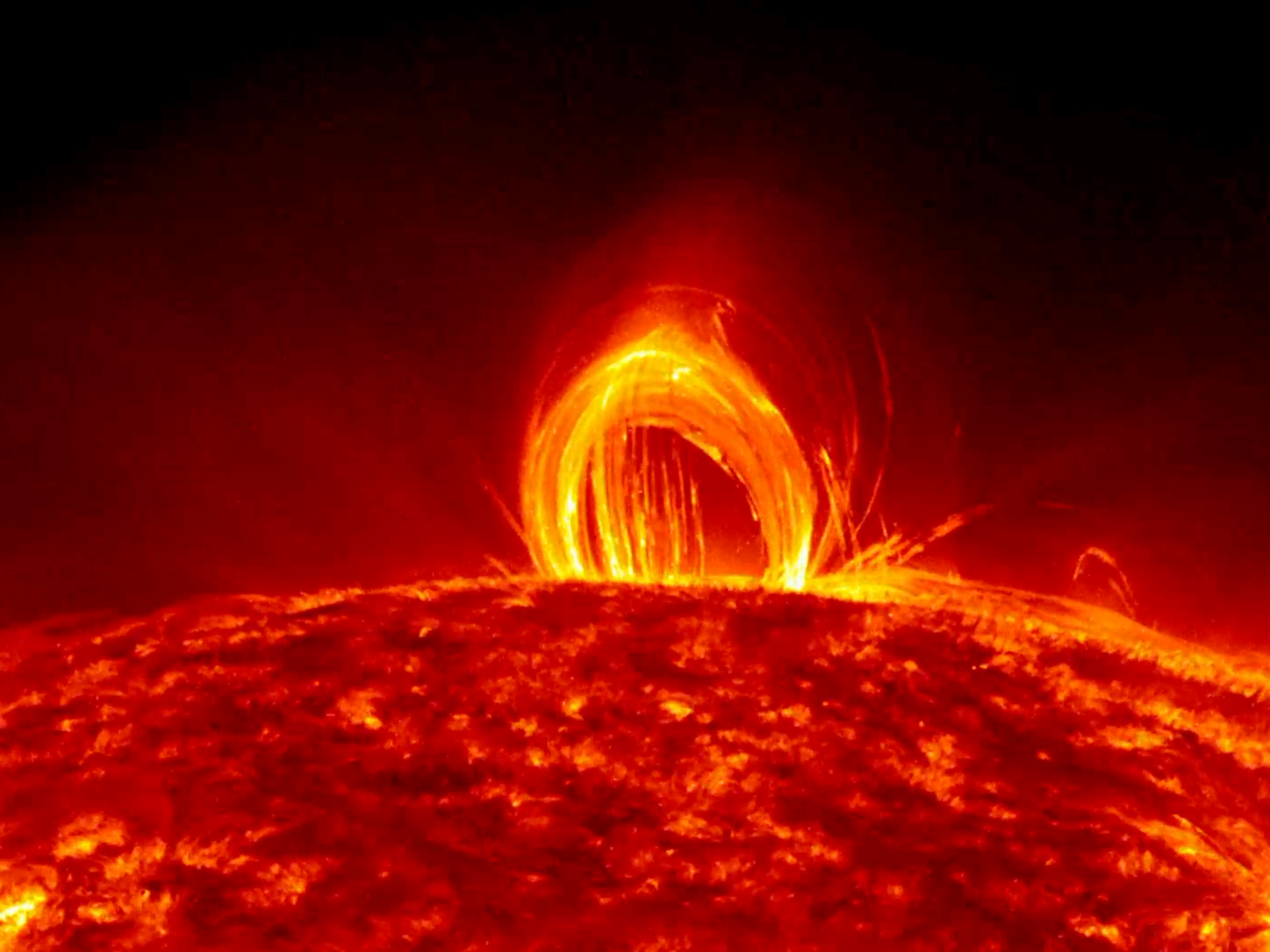
# Plasmas: The Sun- Earth Connection

Jacob Trier Frederiksen

Niels Bohr International  
Academy

---







---

# Today's Programme

---

- ❖ Part I: Plasmas (“classical” electro-magnetic plasmas)
- ❖ Part II: The Sun-Earth Plasma Connection
- ❖ Part III: Solar Storms, Revisited & Modelled
- ❖ Part IV: Solving a Puzzle — The Road Ahead



*“Classical” Electromagnetic Plasmas*

---

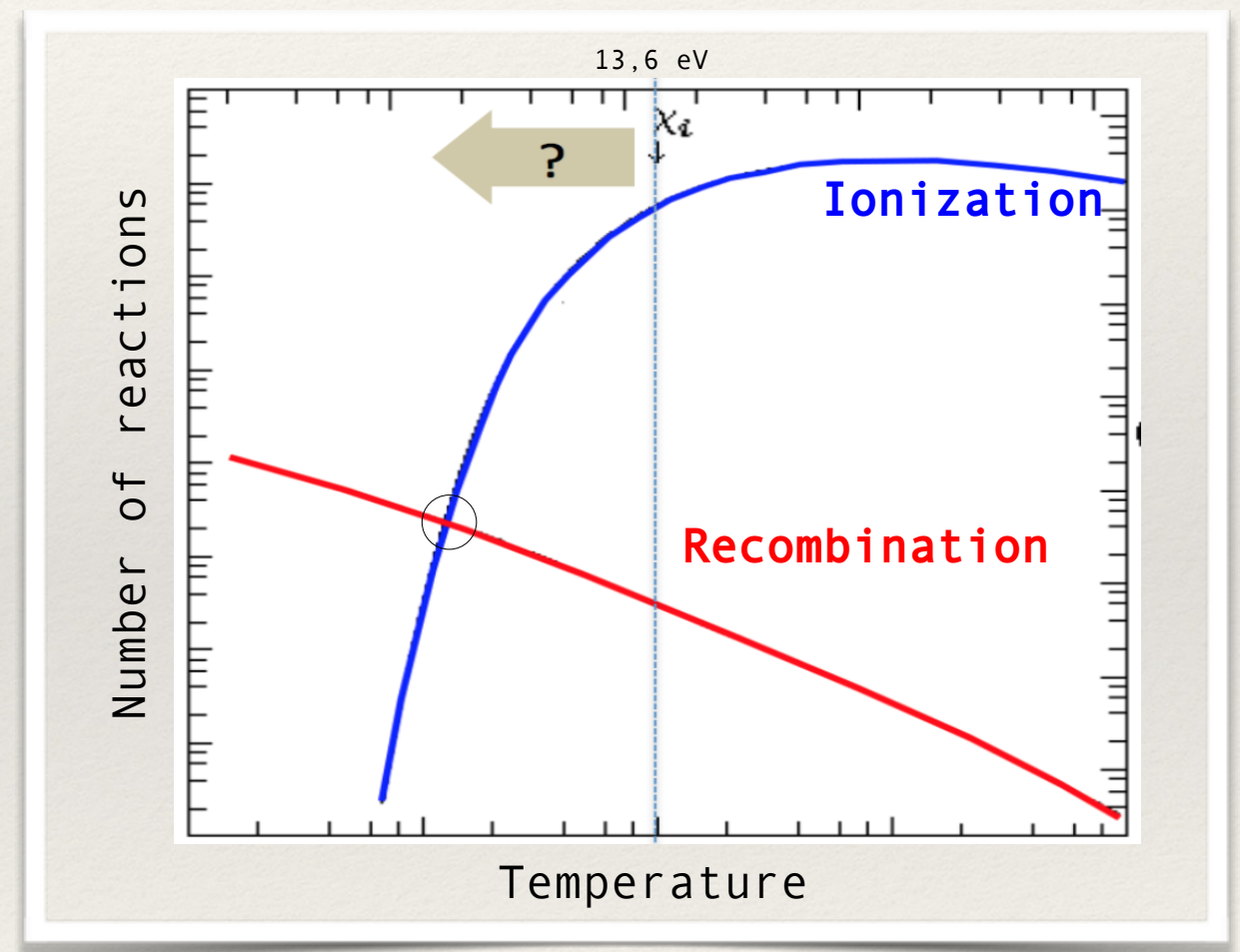
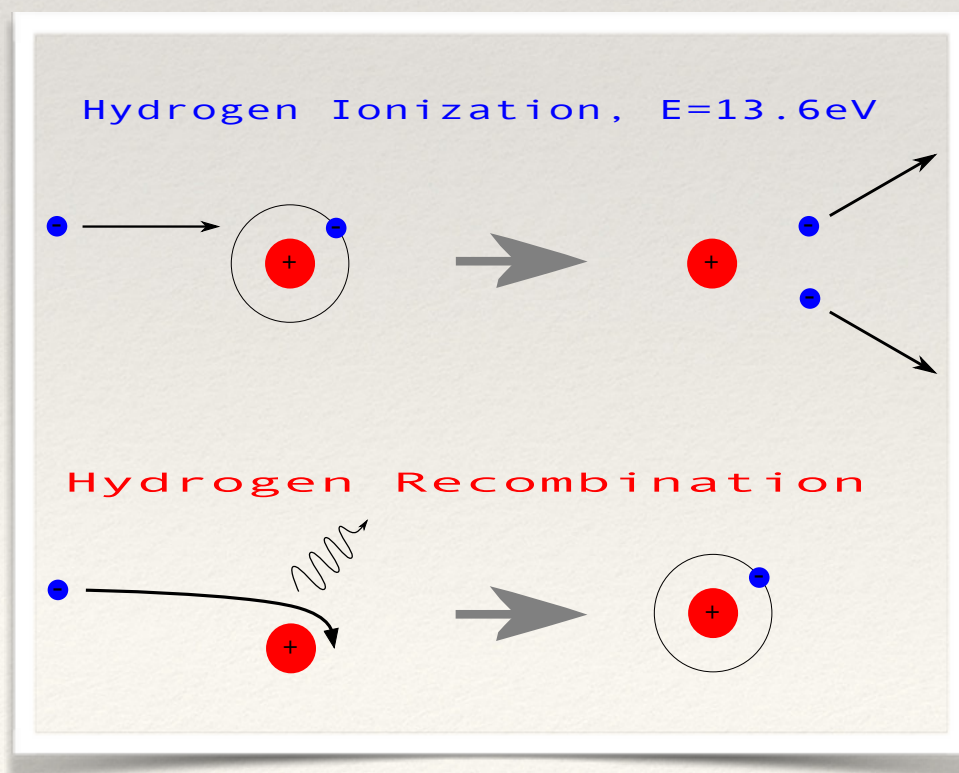
# Part I

- Ionized gases
  - Plasmas in the Universe
  - Plasmas physical descriptions
-



# Plasmas: Ionized Gases.

- ❖ Partially or fully ionized gases.
- ❖ Free electrons and nuclei.
- ❖ Highly electrically conducting.
- ❖ “Gas” can be magnetized.





# Plasmas: A Fourth State of Matter?

Solids



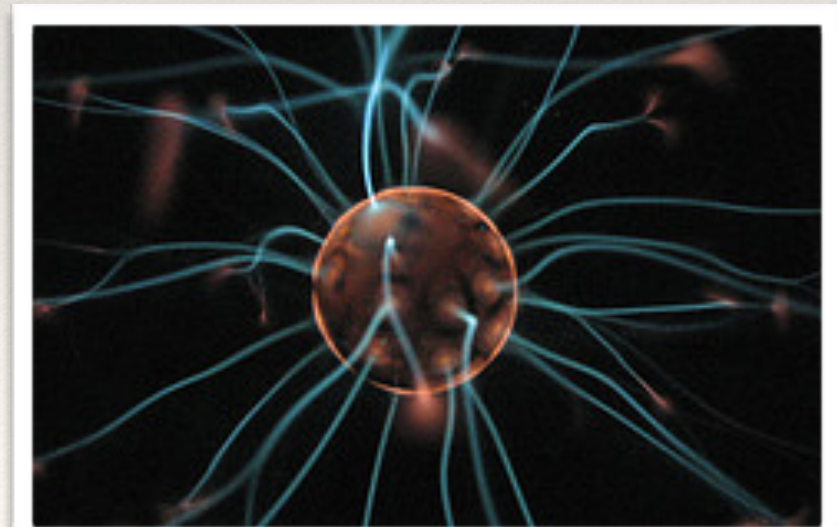
Fluids



Gases

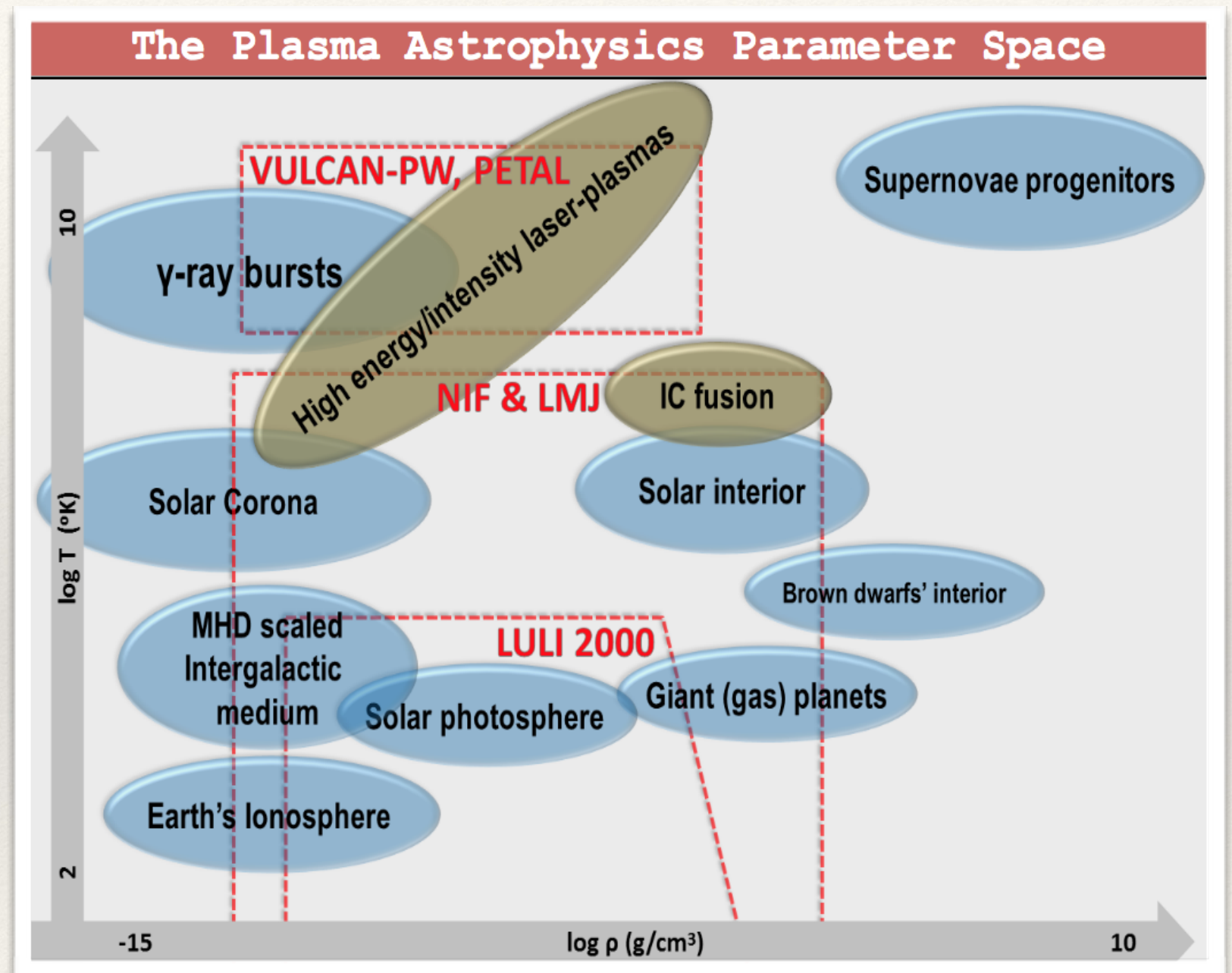
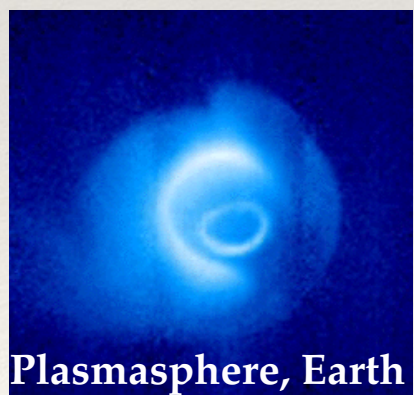
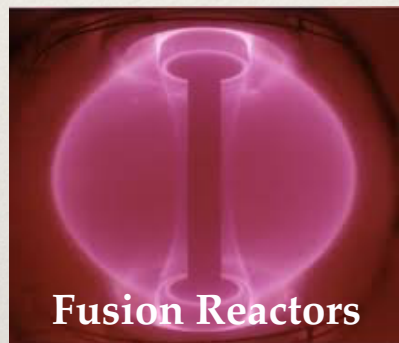
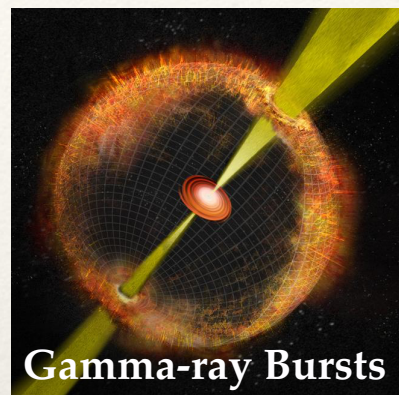
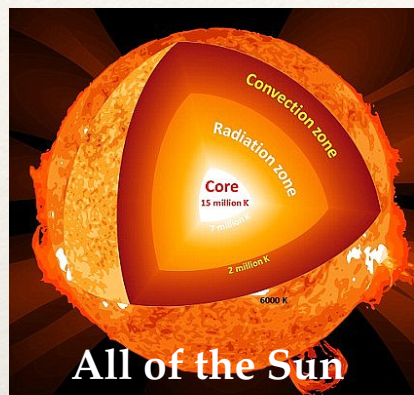


Plasmas



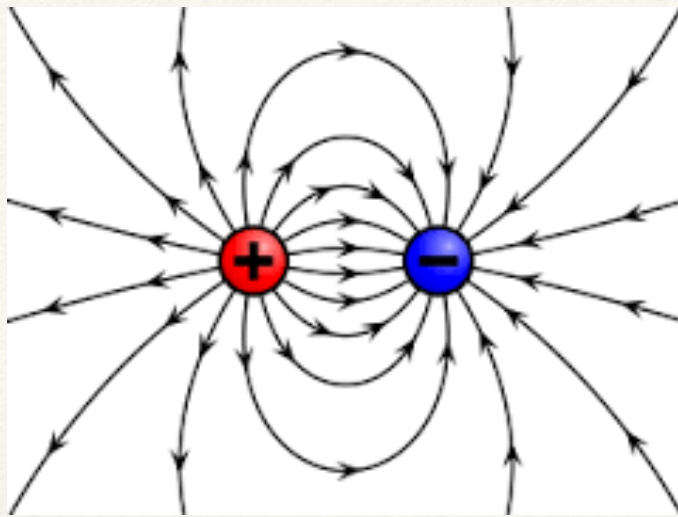


# Plasmas: where do we find them?

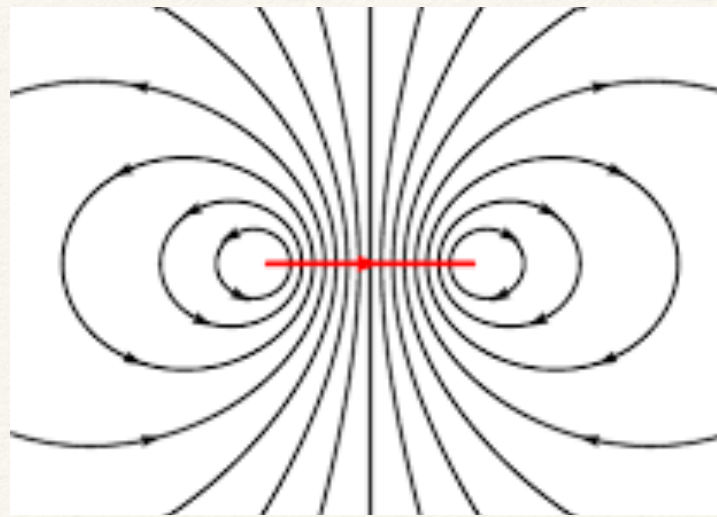


- ❖ Everywhere
- ❖ More than 90% visible baryonic matter likely in plasma state

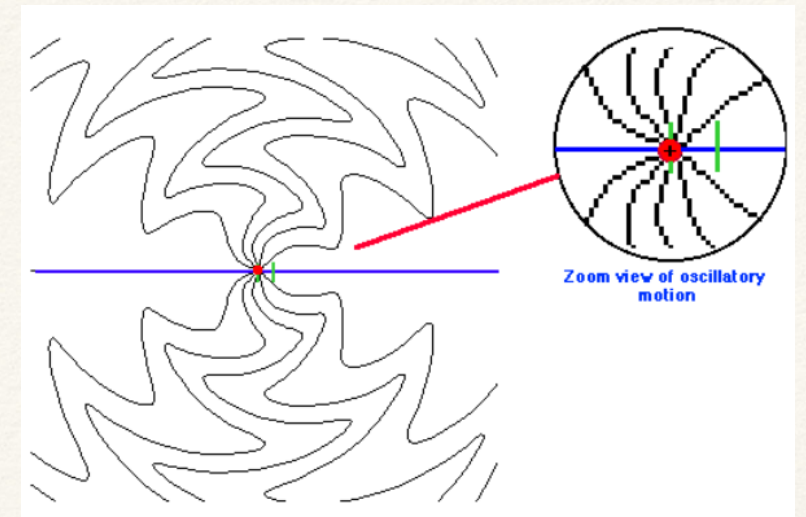




Electricity



Magnetism



Electromagnetism

$$\nabla \cdot \mathbf{B} = 0$$

$$\nabla \cdot \mathbf{E} = \frac{4\pi\rho_c}{\epsilon_0}$$

$$\frac{1}{c}\partial_t\mathbf{B} = -\nabla \times \mathbf{E}$$

$$\frac{\epsilon_0}{c}\partial_t\mathbf{E} = \frac{1}{\mu_0}\nabla \times \mathbf{B} - \frac{4\pi}{c}\mathbf{J}$$

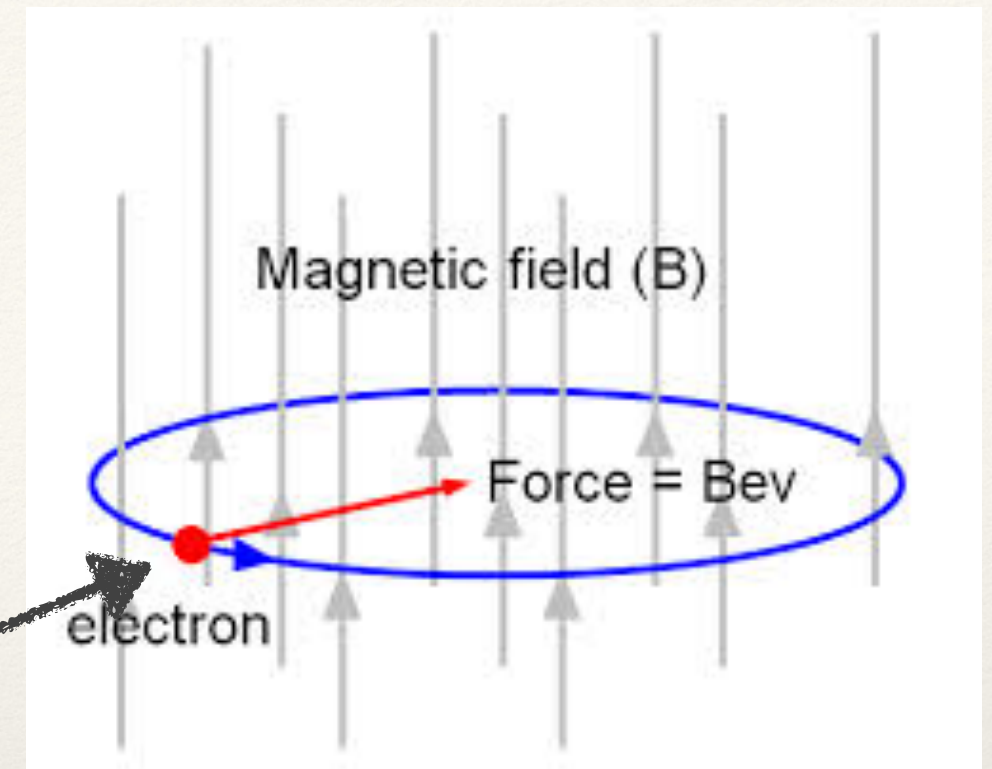
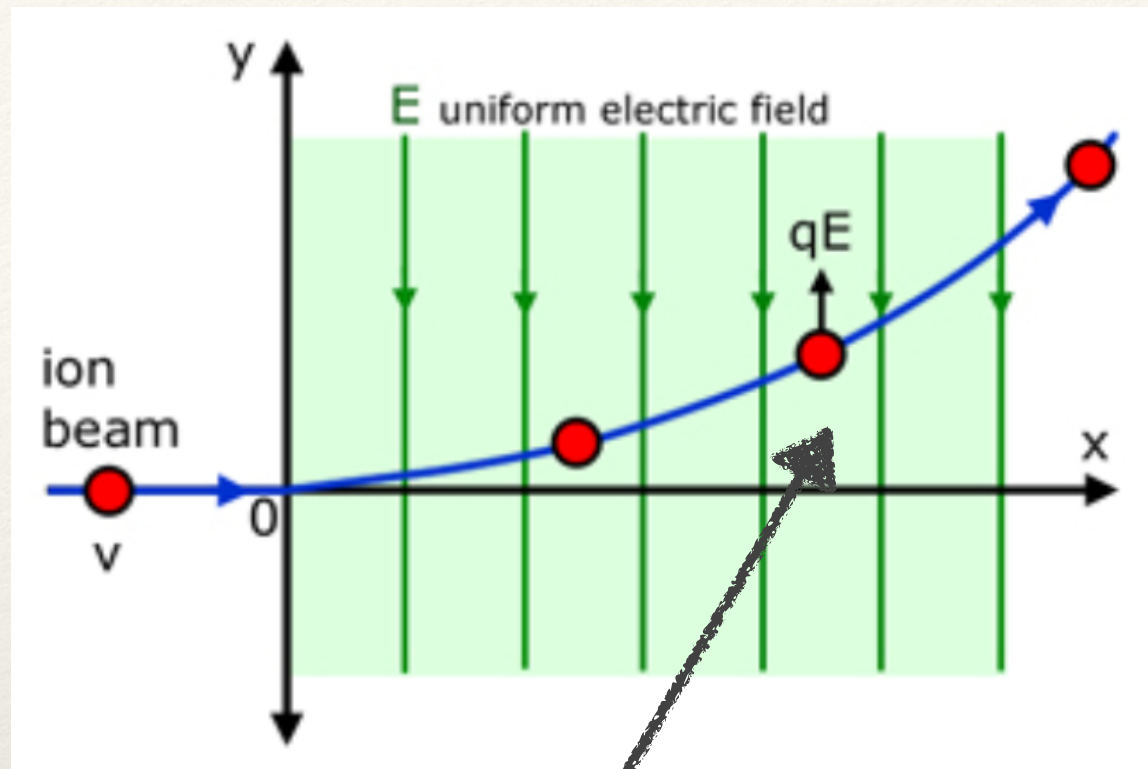
*Charged Particle Fields*

# Plasmas: How Can We Describe Them?

Charged particles have an electric field,  $\mathbf{E}$ , and a magnetic field,  $\mathbf{B}$ , if they move and are accelerated.

We need Maxwell's Equations





$$\mathbf{F}_{L,s} = \frac{d\mathbf{p}}{dt} = q_s(\mathbf{E} + \frac{1}{c}\mathbf{v} \times \mathbf{B}) \quad [+m_s\mathbf{g} + \dots]$$

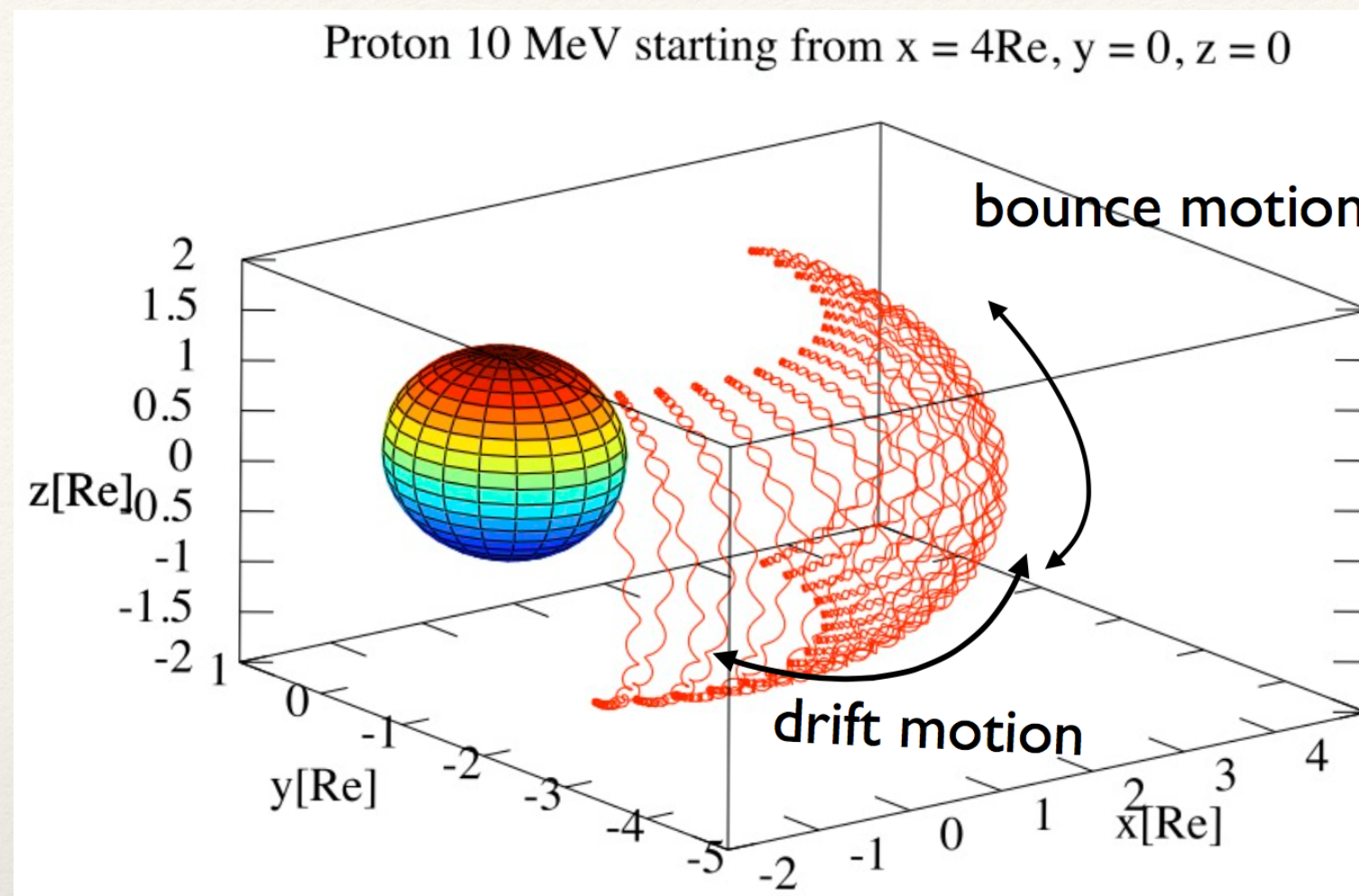
$$\mathbf{p}_s = m_s\mathbf{v}\gamma(v) = \frac{m_s\mathbf{v}_s}{\sqrt{1-\beta^2}}$$

*Charged Particle Motion*

# Plasmas: How Can We Describe Them?

Charged Particles can be forced by electric and magnetic fields.  
We need the Lorentz Force.





Earth's magnetosphere modeled with magnetic dipole

### *Charged Particle Motion*

# Plasmas: How Can We Describe Them?

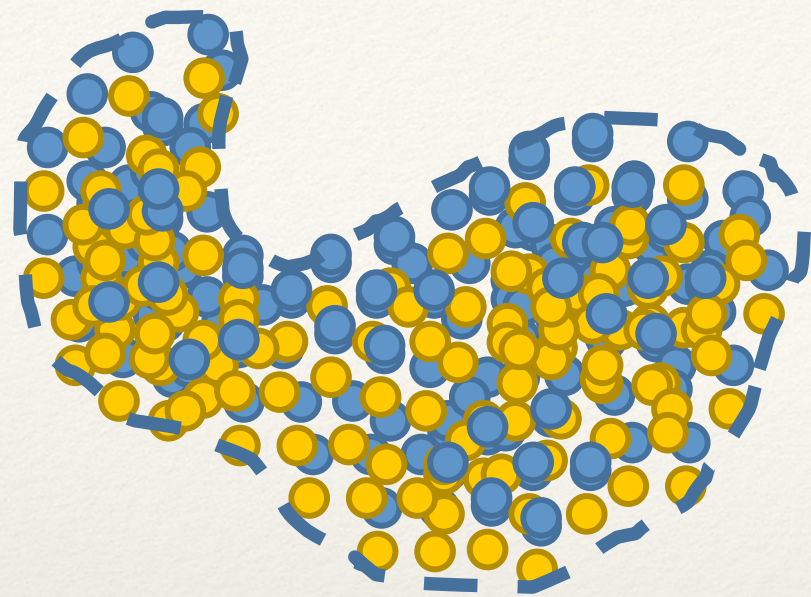
Charged Particles will generally experience drift in electromagnetic fields and EM fields with gradients.



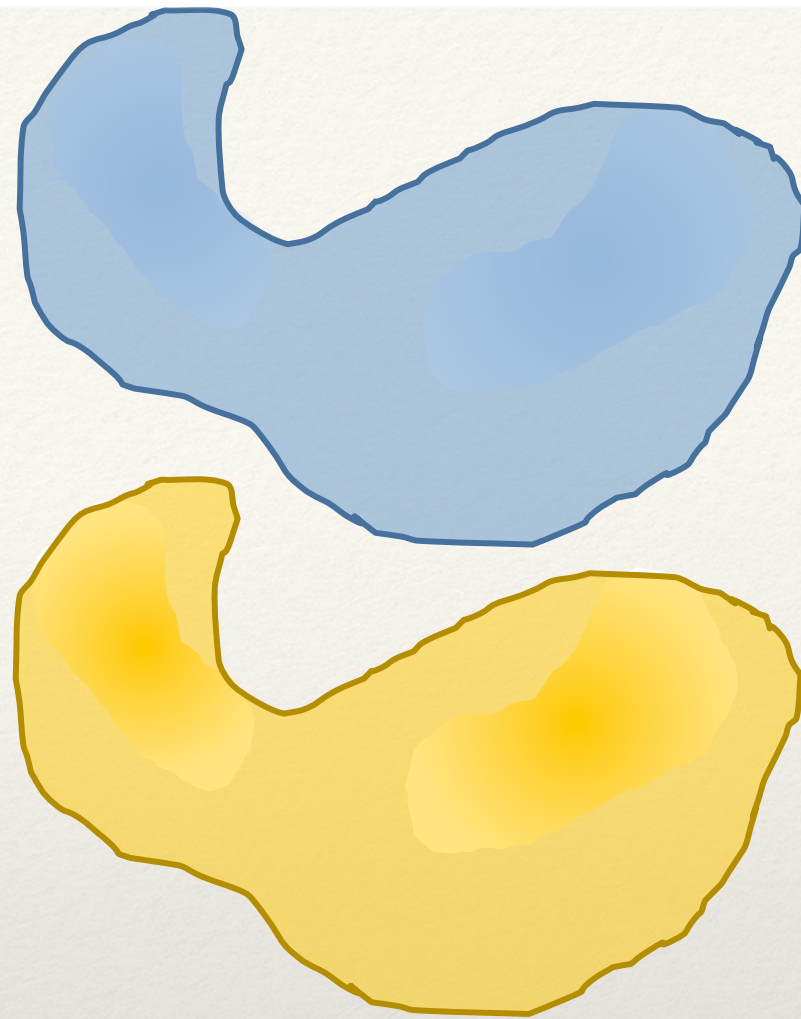
“OK, that was one particle — but a plasma is  
MANY particles?!?”

*Yes.*





N-particle plasma ( $N \gg 1$ ), say, e + p



$f_s(\mathbf{r}, \mathbf{p}, t)$  == one-particle PDFs, species 's'

*Many particles we can make into a continuum particle distribution*

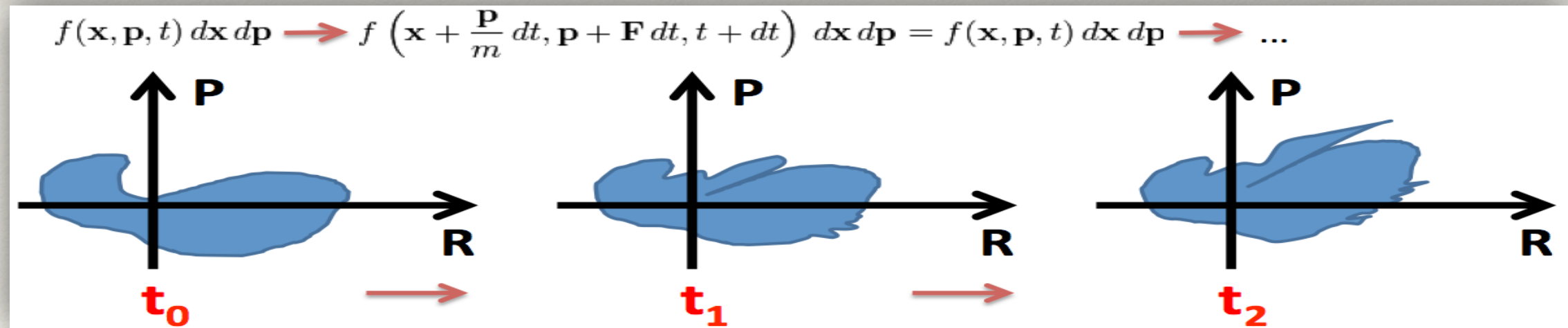
# Plasmas: Many-particle systems

Consider many particles!

They are now *almost* a continuum.

We can define macroscopic variables,  $J$  and  $\rho$  (charge density).





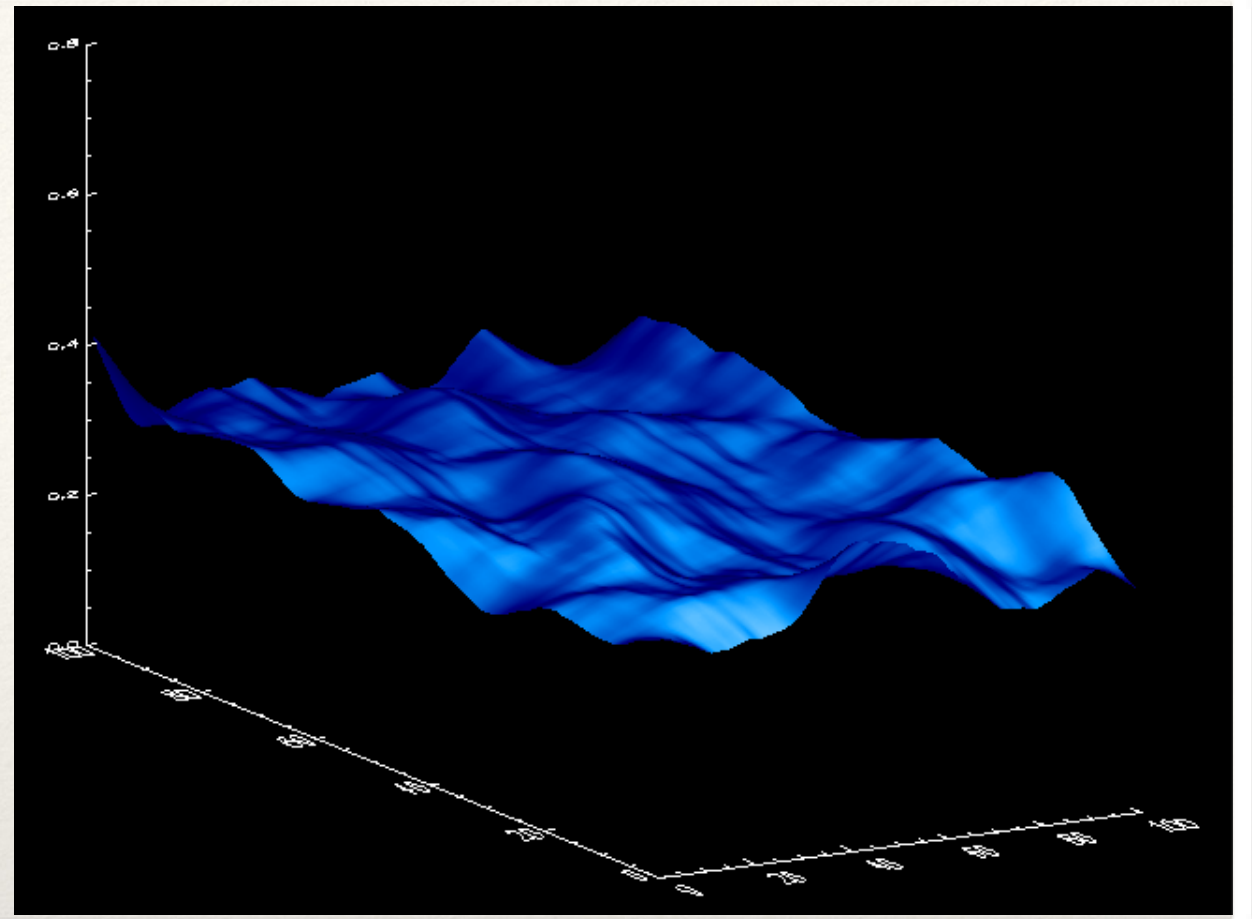
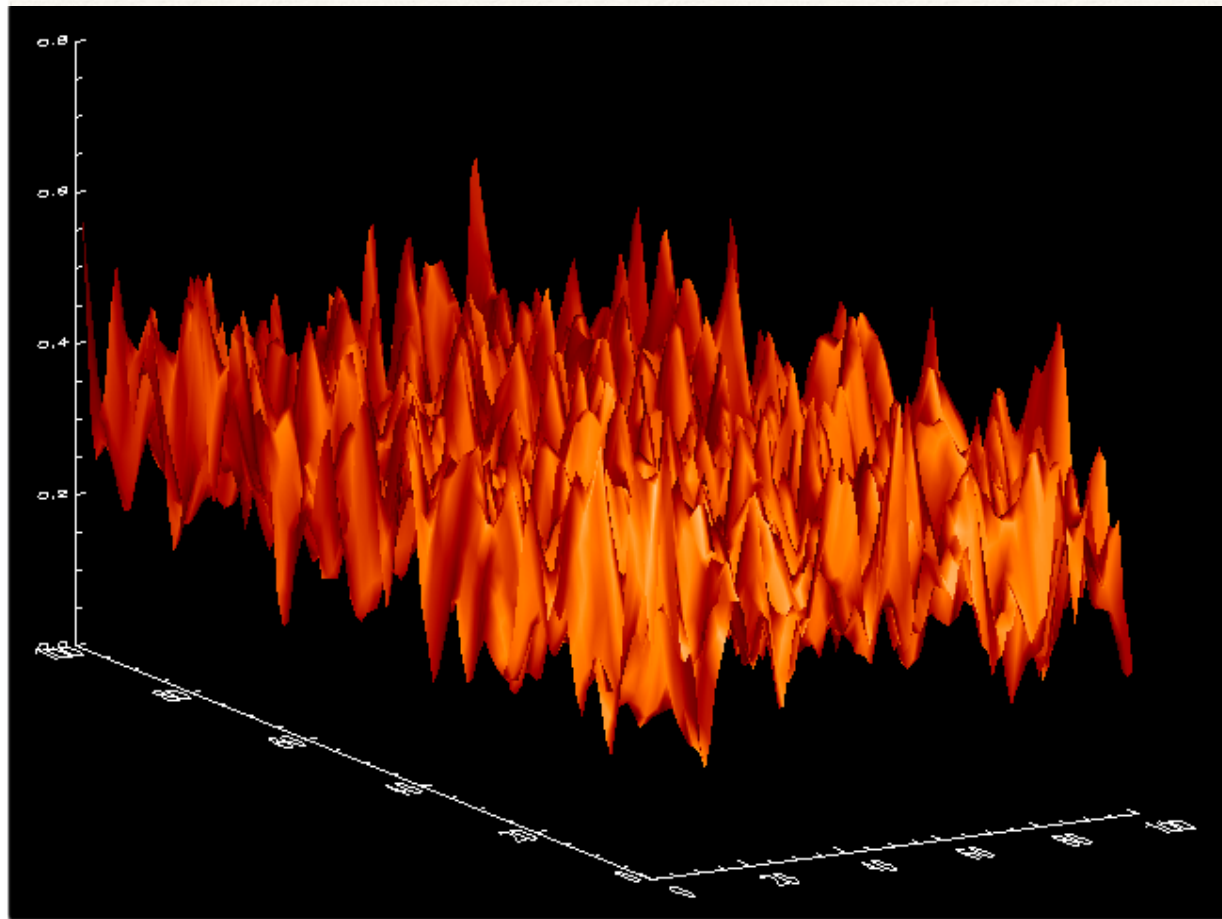
$$\frac{\partial f^i}{\partial t} + \frac{\mathbf{p}}{m^i} \cdot \frac{\partial f^i}{\partial \mathbf{x}} + \mathbf{F} \cdot \frac{\partial f^i}{\partial \mathbf{p}^i} = \left. \frac{\partial f^i}{\partial t} \right|_{coll}$$

Almost there....

# Plasmas: the Boltzmann Equation

Describes how a distribution (of many, many, particles) evolves with time under forcing.





*Assume collective behavior, smooth away all particle-particle (direct) interactions*

# Plasmas: the Vlasov Contribution

Vlasov's point of view:  
Electromagnetic fields are smooth mean fields produced collectively and self-consistently by all particles (+ext fields).



$$\frac{\partial f^i}{\partial t} + \mathbf{u} \cdot \frac{\partial f^i}{\partial \mathbf{x}} + \frac{q^i}{m^i} (\mathbf{E} + \mathbf{u}_i \times \mathbf{B}) \cdot \frac{\partial f^i}{\partial (\mathbf{u}\gamma)^i} = \frac{\partial f^i}{\partial t} \Big|_{coll} \quad \left. \begin{array}{l} \text{Vlasov} \\ \text{Schep} \end{array} \right\} \text{Vlasov-Schep}$$

$$-\frac{\partial \mathbf{B}}{\partial t} = \nabla \times \mathbf{E}$$

$$\nabla \cdot \mathbf{E} = \rho_c$$

$$\frac{1}{c^2} \frac{\partial \mathbf{E}}{\partial t} = \nabla \times \mathbf{B} - \mu_0 \mathbf{J}$$

$$\nabla \cdot \mathbf{B} = 0$$

Maxwell

$$\rho_c(\mathbf{x}) = \sum_i q^i f^i(\mathbf{x}, \mathbf{u})$$

$$\mathbf{J}(\mathbf{x}) = \int d\mathbf{u} \sum_i \mathbf{u} q^i f^i(\mathbf{x}, \mathbf{u})$$

$$\mathbf{J}(\mathbf{x}) = \int d\mathbf{u} \sum_i \mathbf{u} q^i f^i(\mathbf{x}, \mathbf{u})$$

EM Sources

We'll return to these equations later

# Plasmas: the Full-blown Set of Equations for Plasmas

Very very complicated, yet, still a gross approximation.

The 'Vlasov-Maxwell' System



“Gimme a break — Please.”

*[5 minutes]*




## *The Sun-Earth Plasma Connection & Solar Storms*

---

# Part II

- The Sun's magnetic cycle
  - Solar storms
  - Earth's space environment
  - Space weather
  - Climate questions...
-





# Solstorm og nordlys

Måske var De en af de heldige, som natten til den 27. september kunne nyde nordlyset over Danmark. Det skyldtes, at en kraftig solstorm ramte Jordens atmosfære. Stormen, der består af magnetisk ladede partikler, havde sit udspring i et udbrud fra solplet nummer 1302 i mandags. Solpletten har allerede haft to tidligere udbrud den 22. og 24. september.

*"Today's Space Weather"*

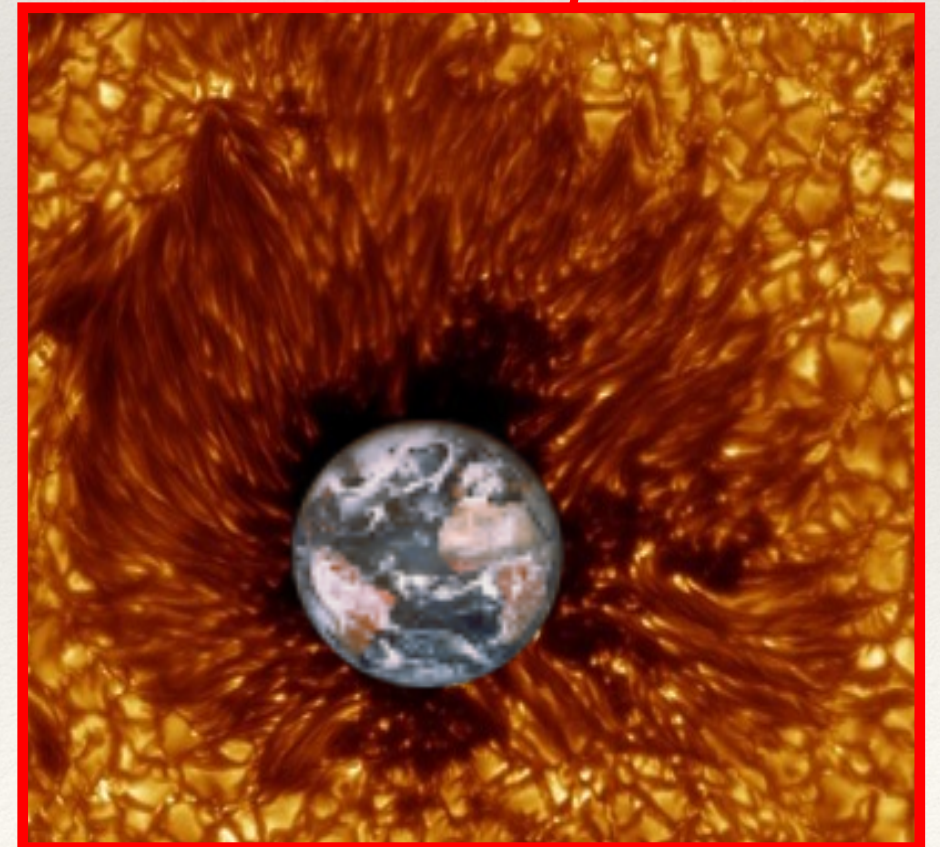
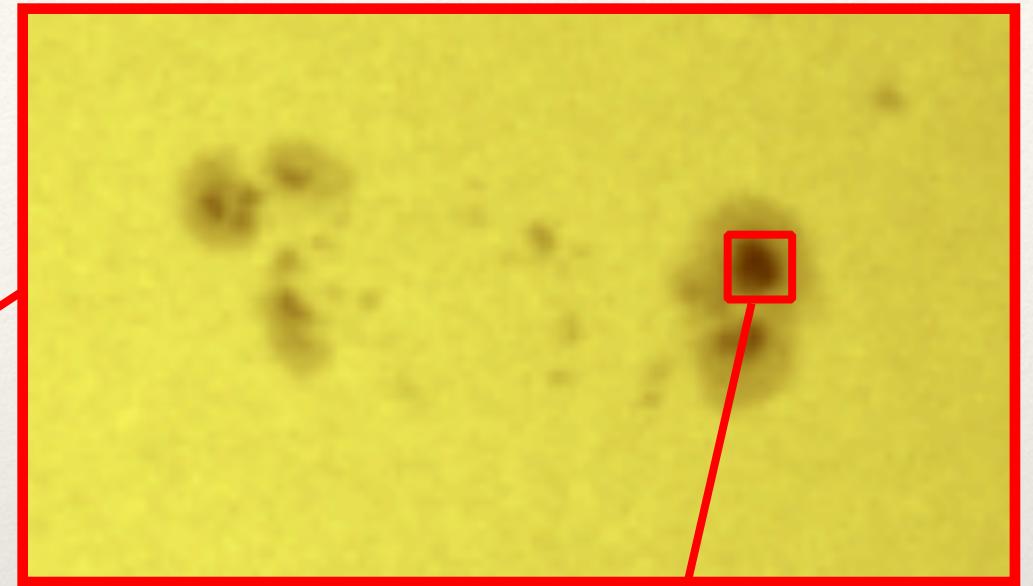
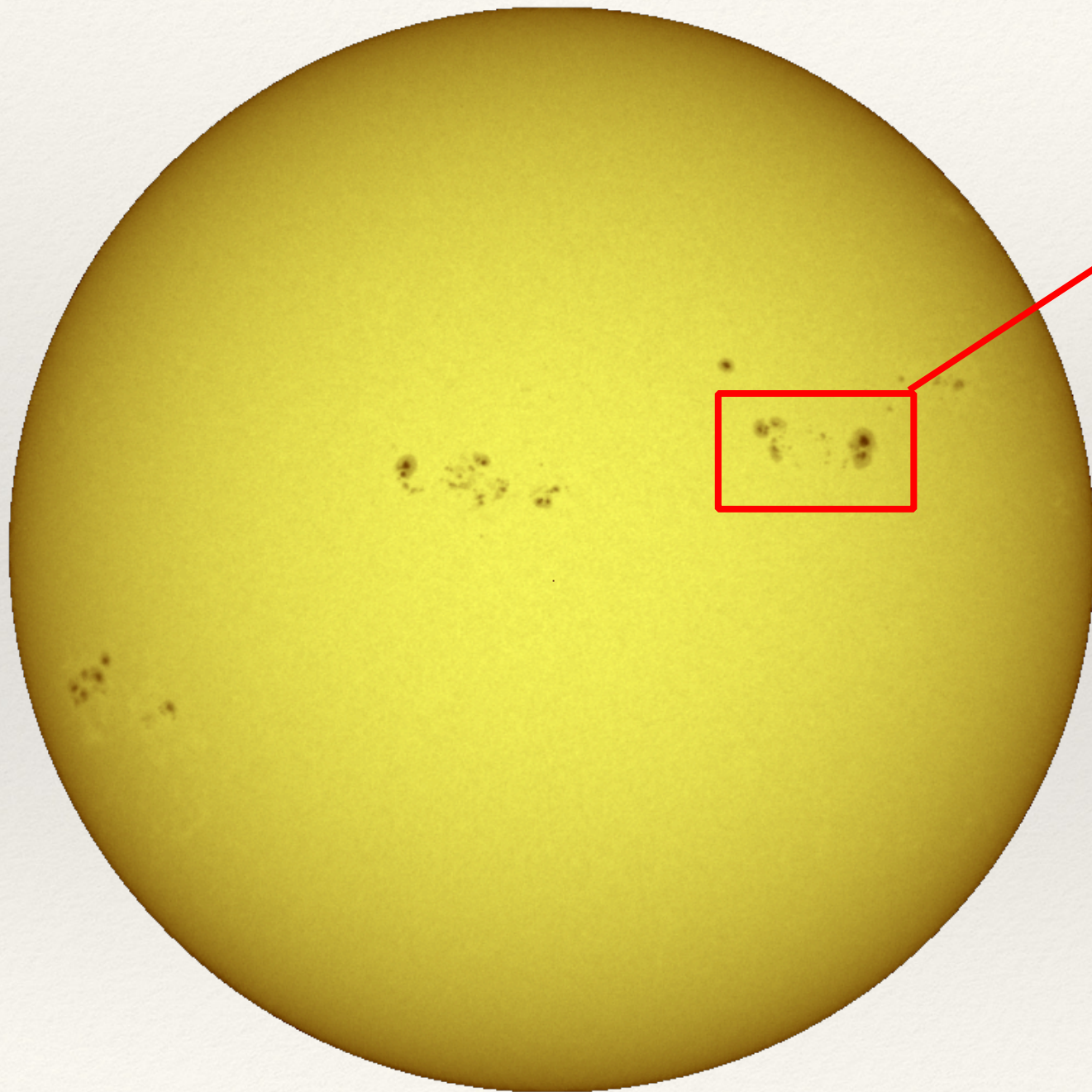
## Danish Media

One-half Solar Cycle Ago...

Cycle #24 approaching peak  
in '13-'14-ish..



# The Sun's “Surface” - The Photosphere

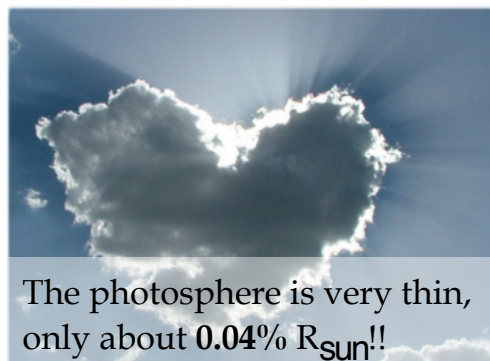
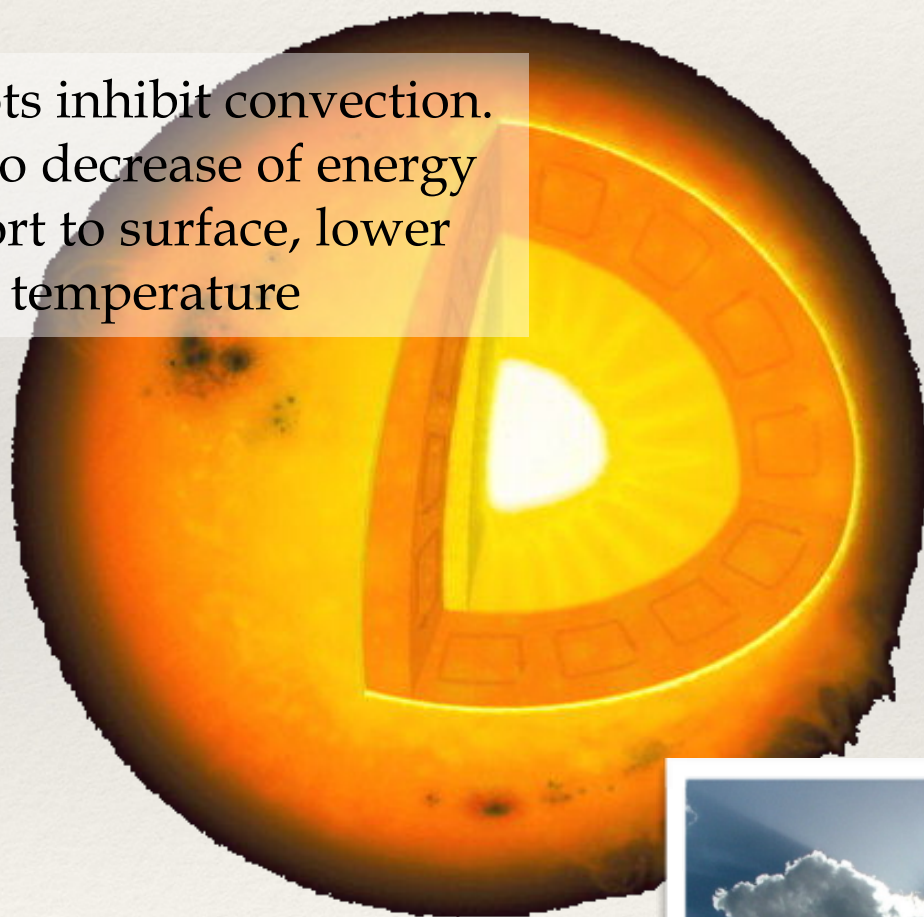




# Our Star

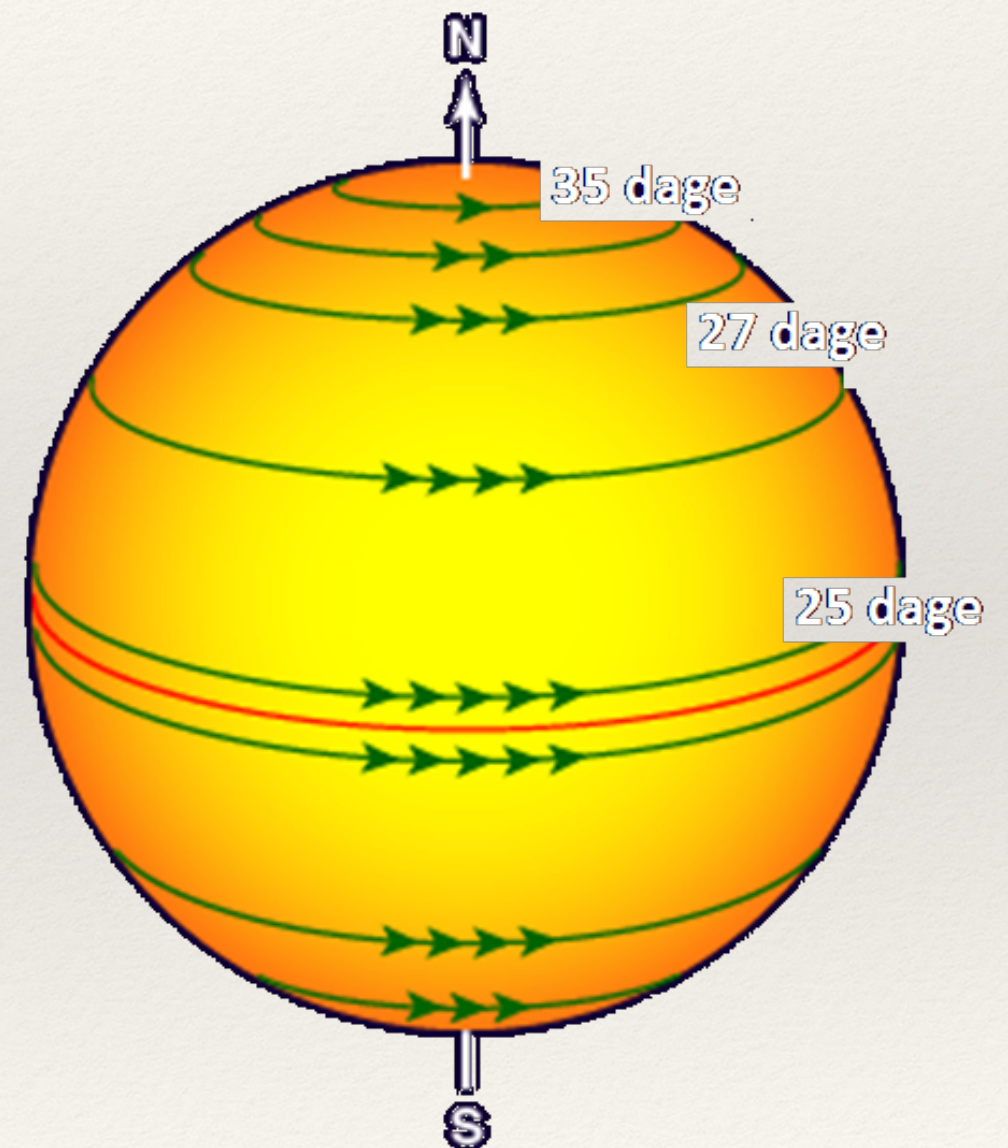
## Stellar Structure of the Sun

Sunspots inhibit convection.  
Leads to decrease of energy  
transport to surface, lower  
surface temperature



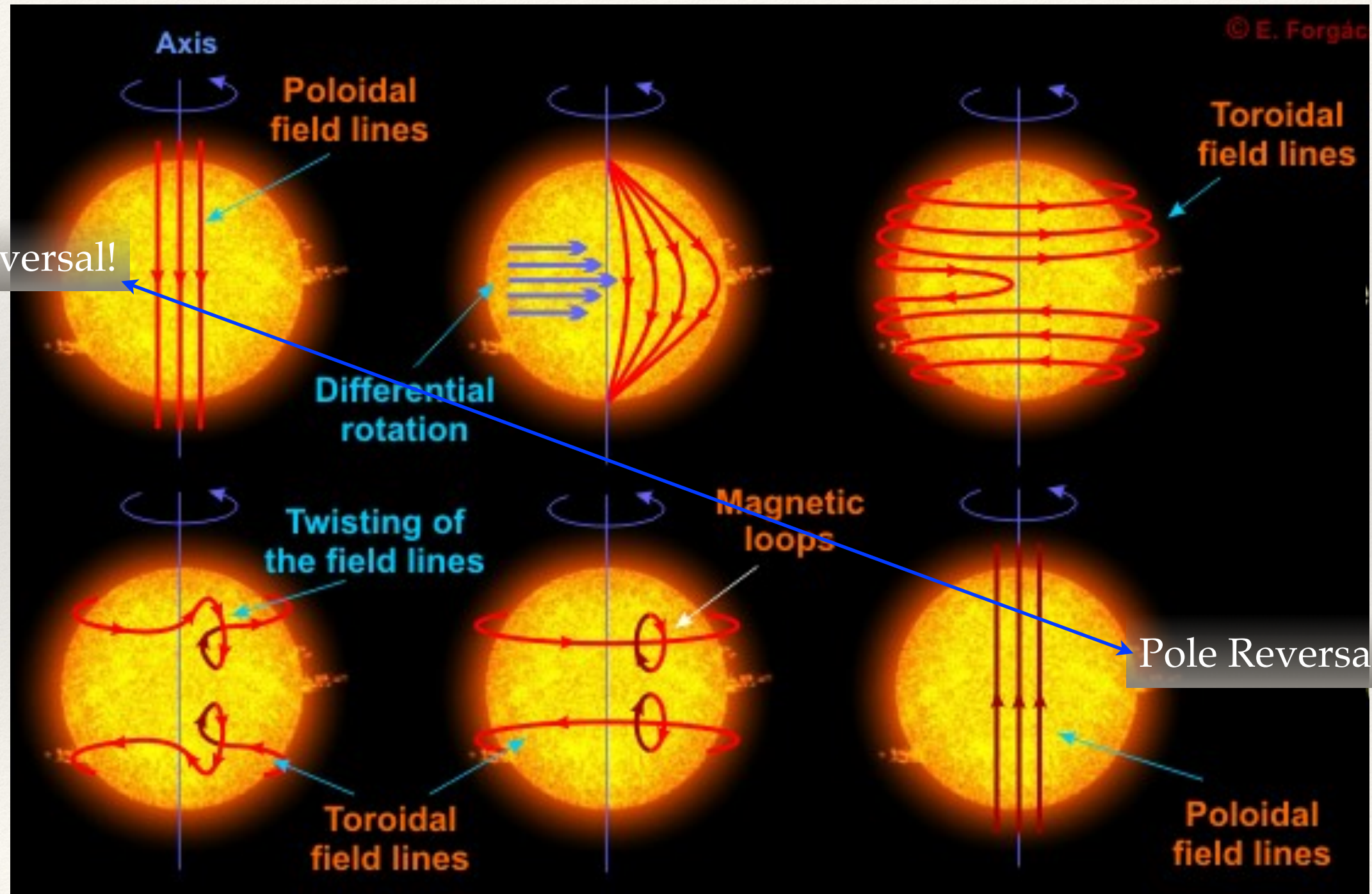
The photosphere is very thin,  
only about 0.04%  $R_{\text{sun}}$ !!

## The Sun's Surface Rotation





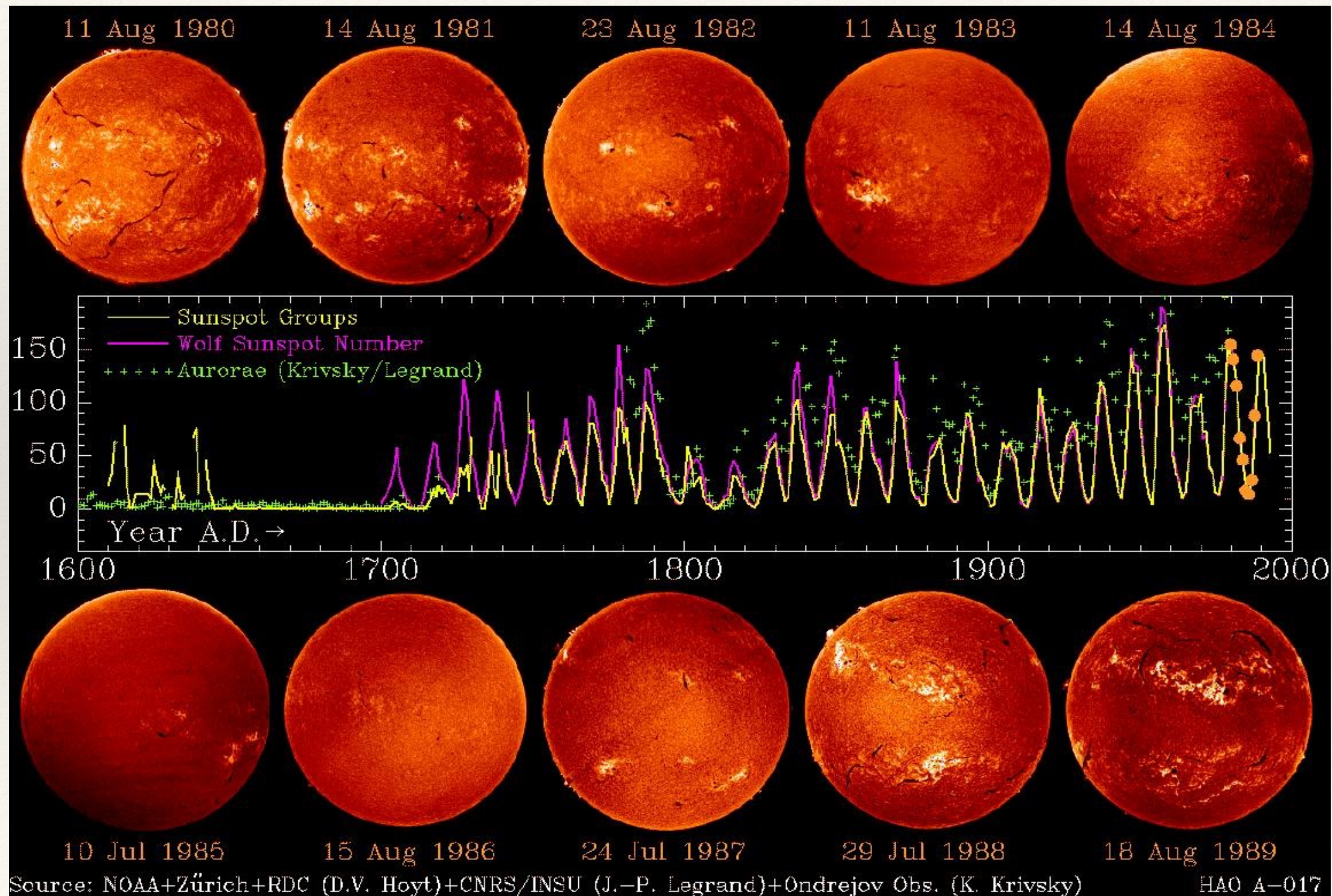
# Theory of Sun Spot Generation





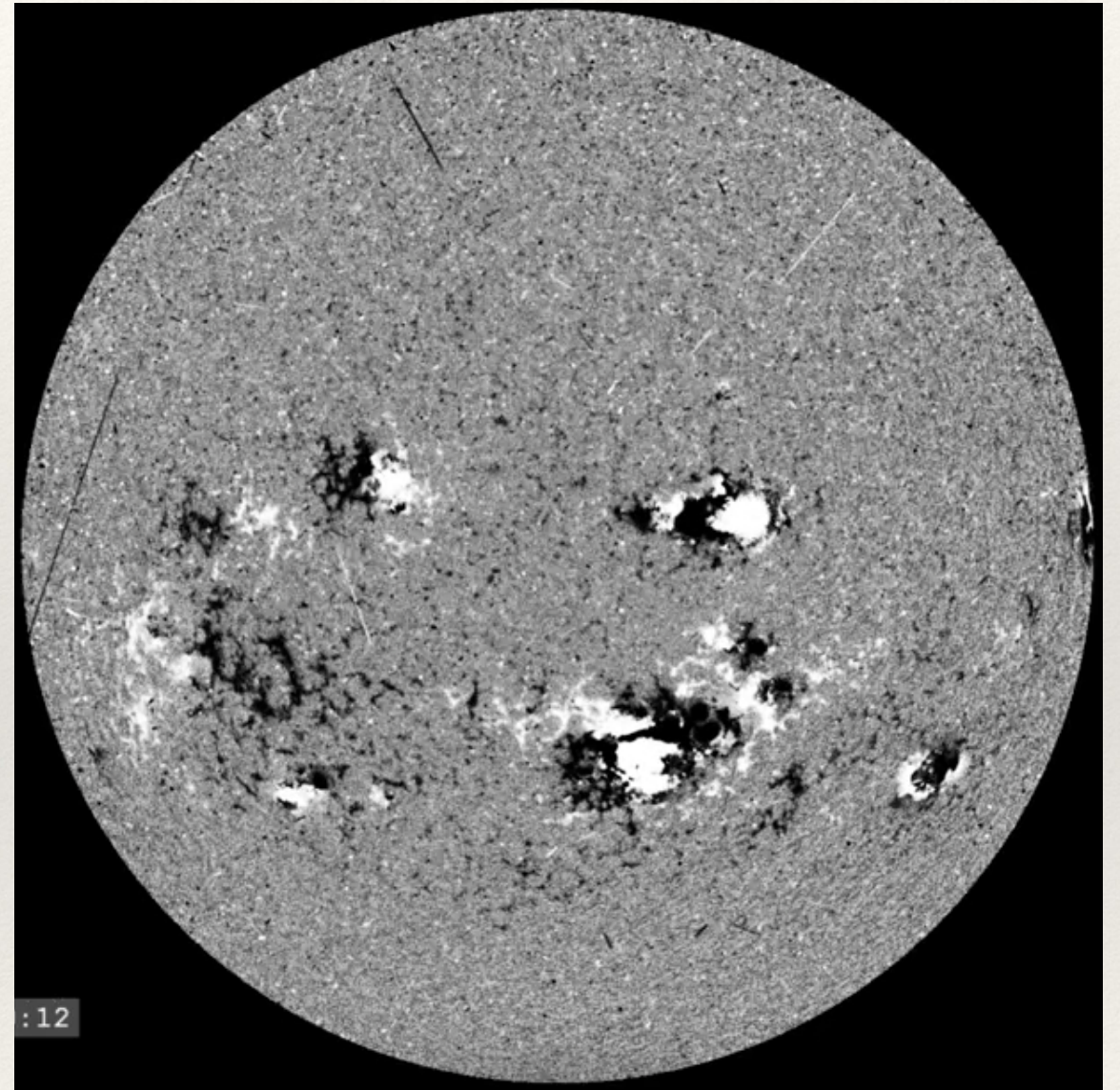
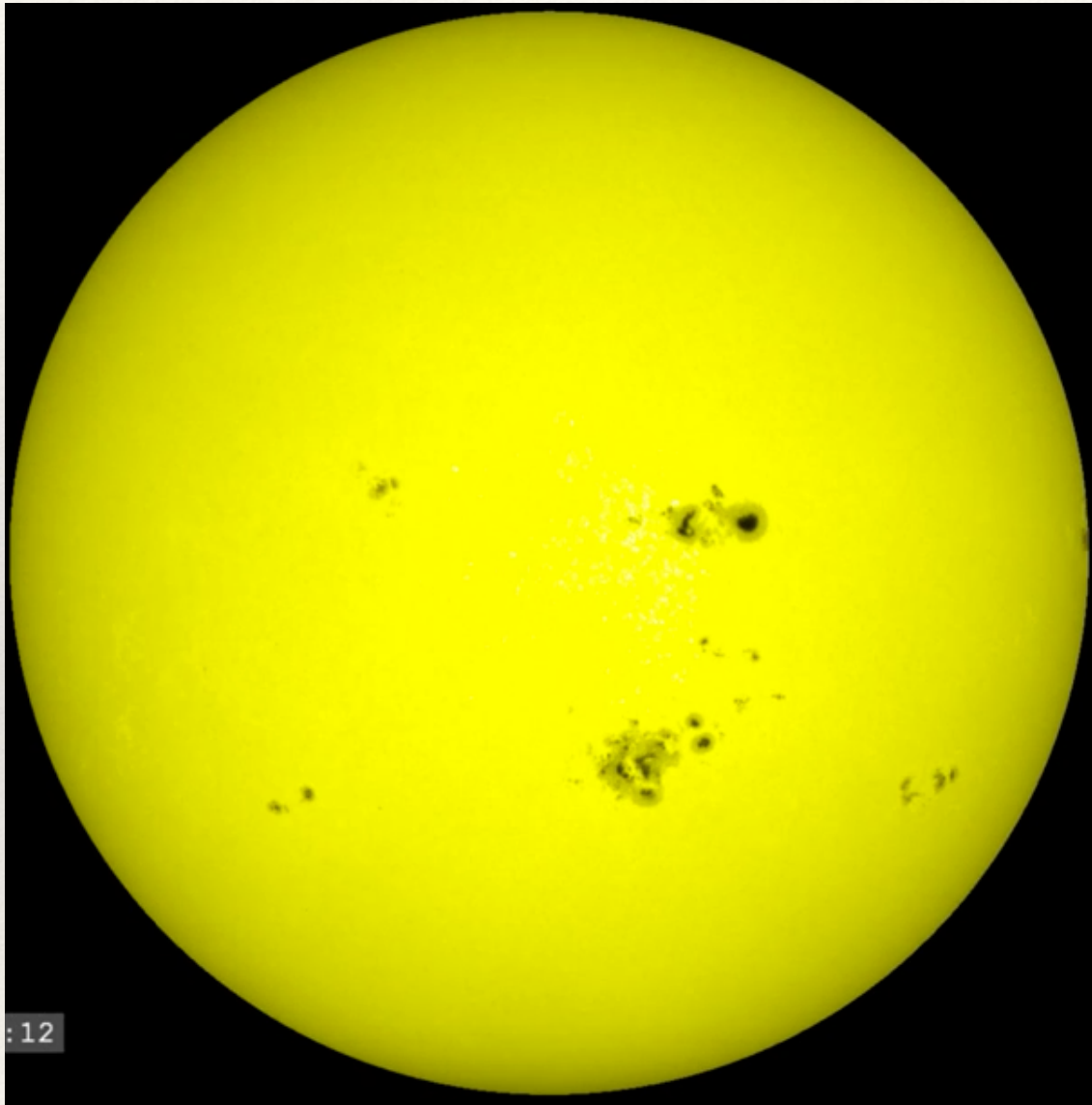
# Sunspots — A (very) Brief History...

Cycles #21 & #22 (max-to-max)



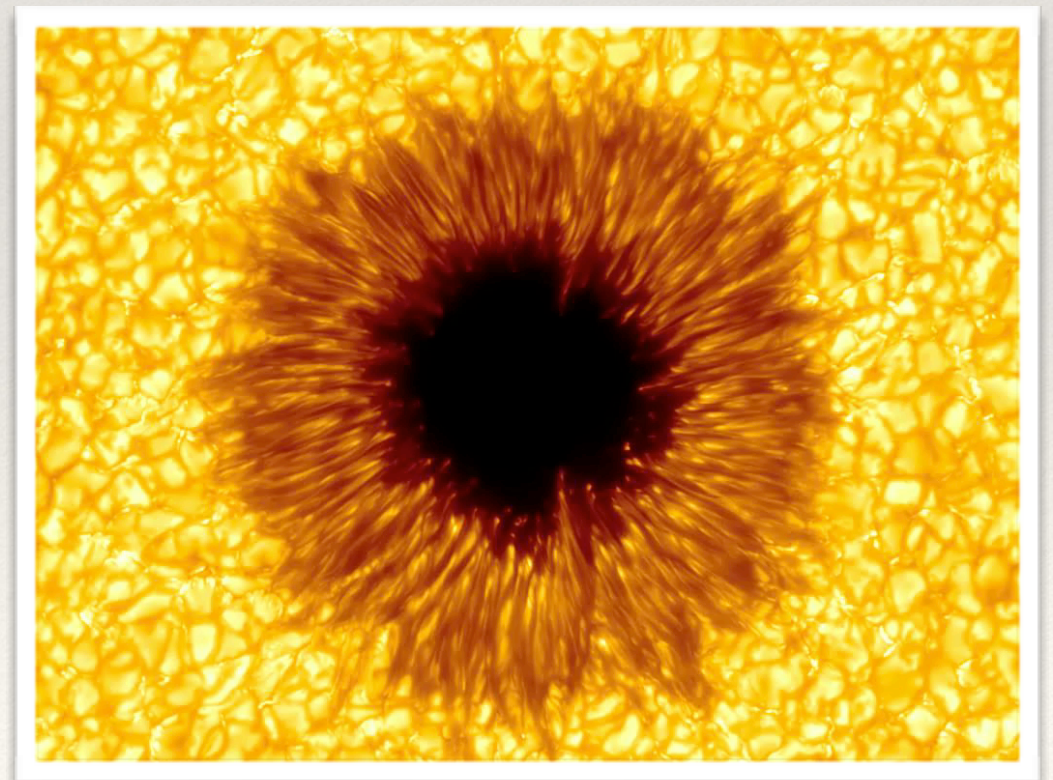
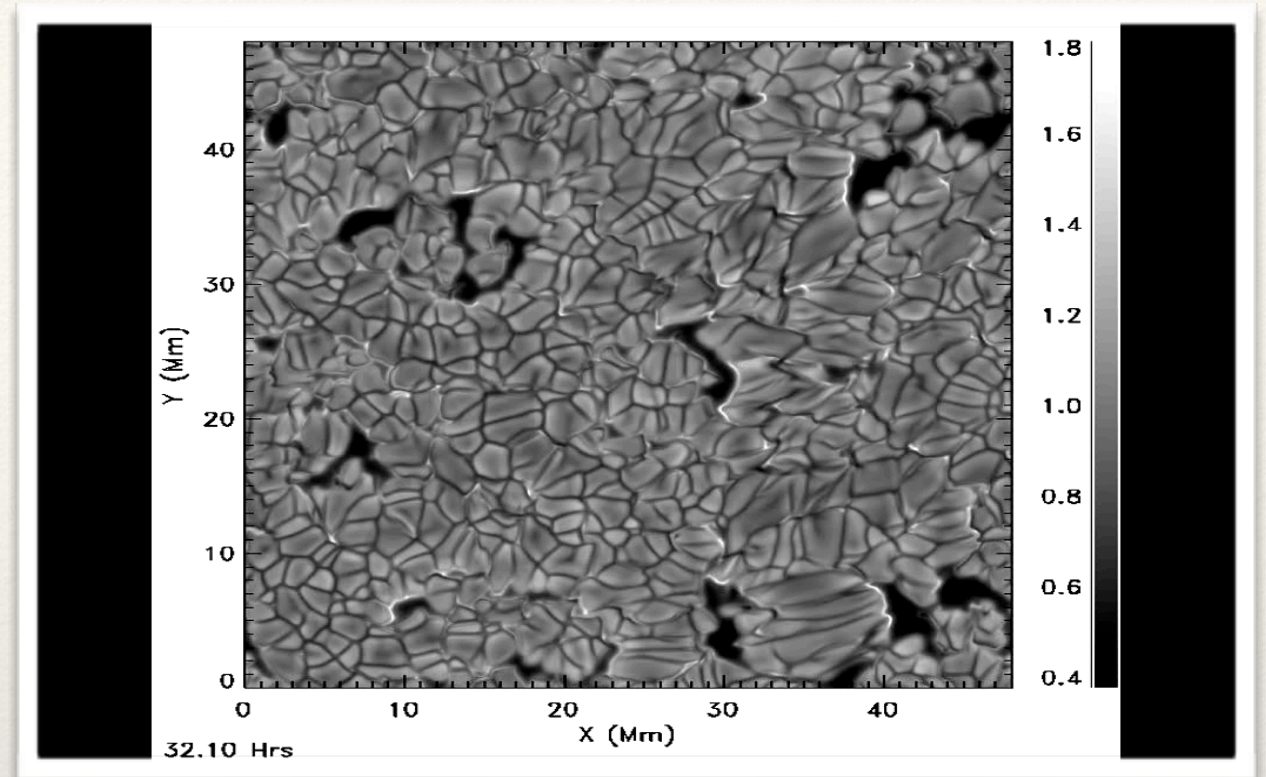


# Sunspots = Magnetic Flux Emergence



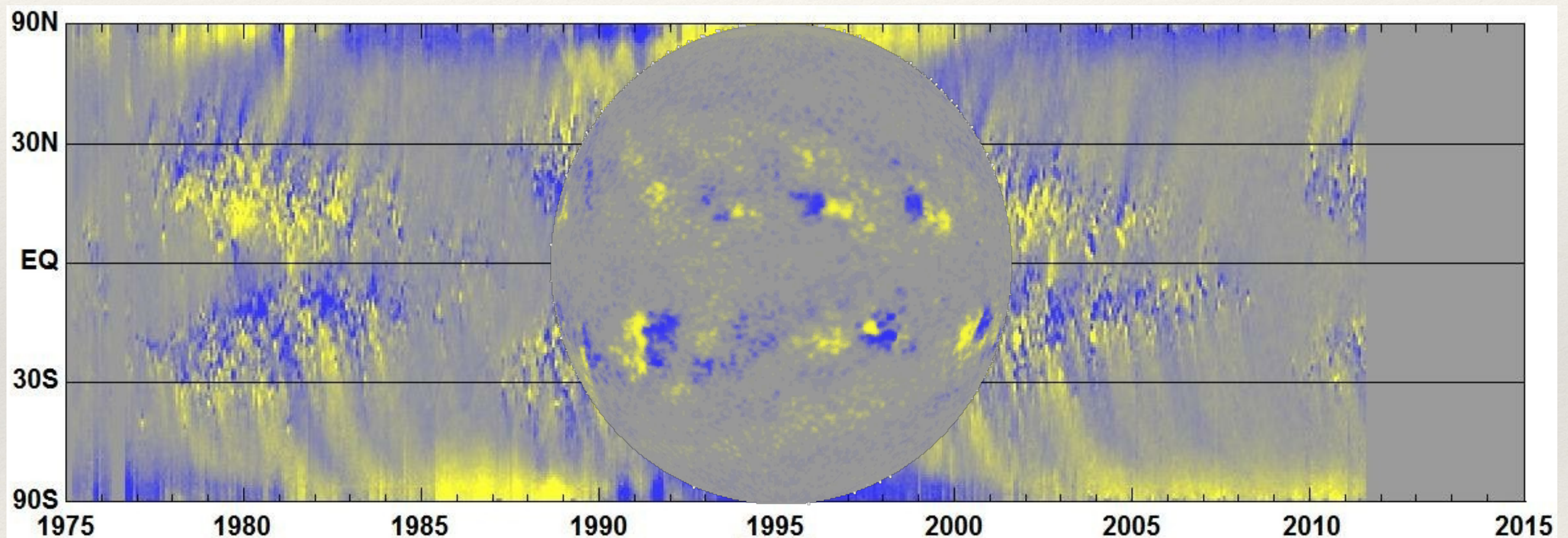


# Sunspots = Magnetic Flux Emergence





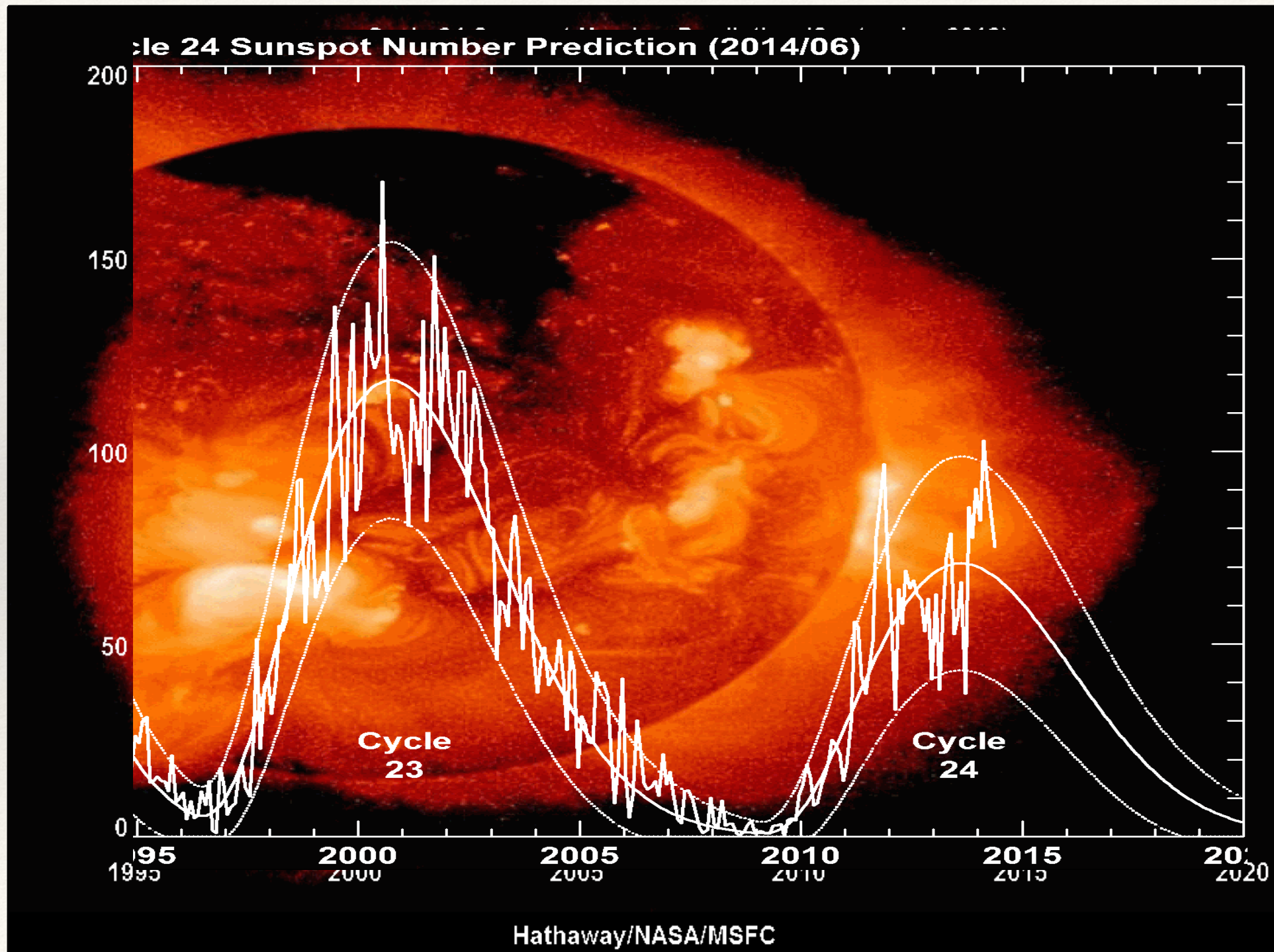
# Solar Cycles — Deconvolved



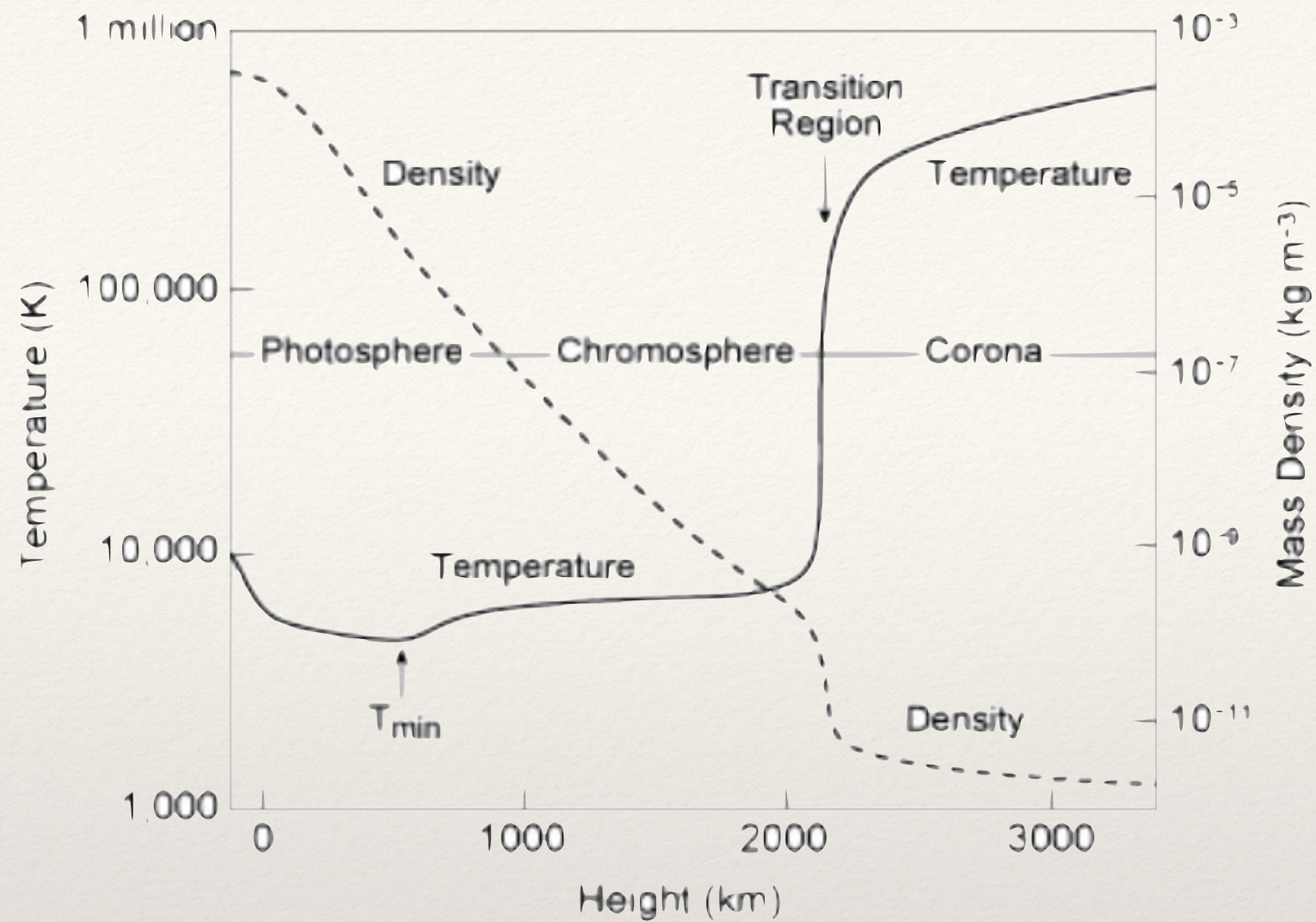
Credit: D. Hathaway, NASA



# Solar Cycle #24 – Maximum Prediction Revisited







*Extreme Profile*

# The Solar Atmosphere

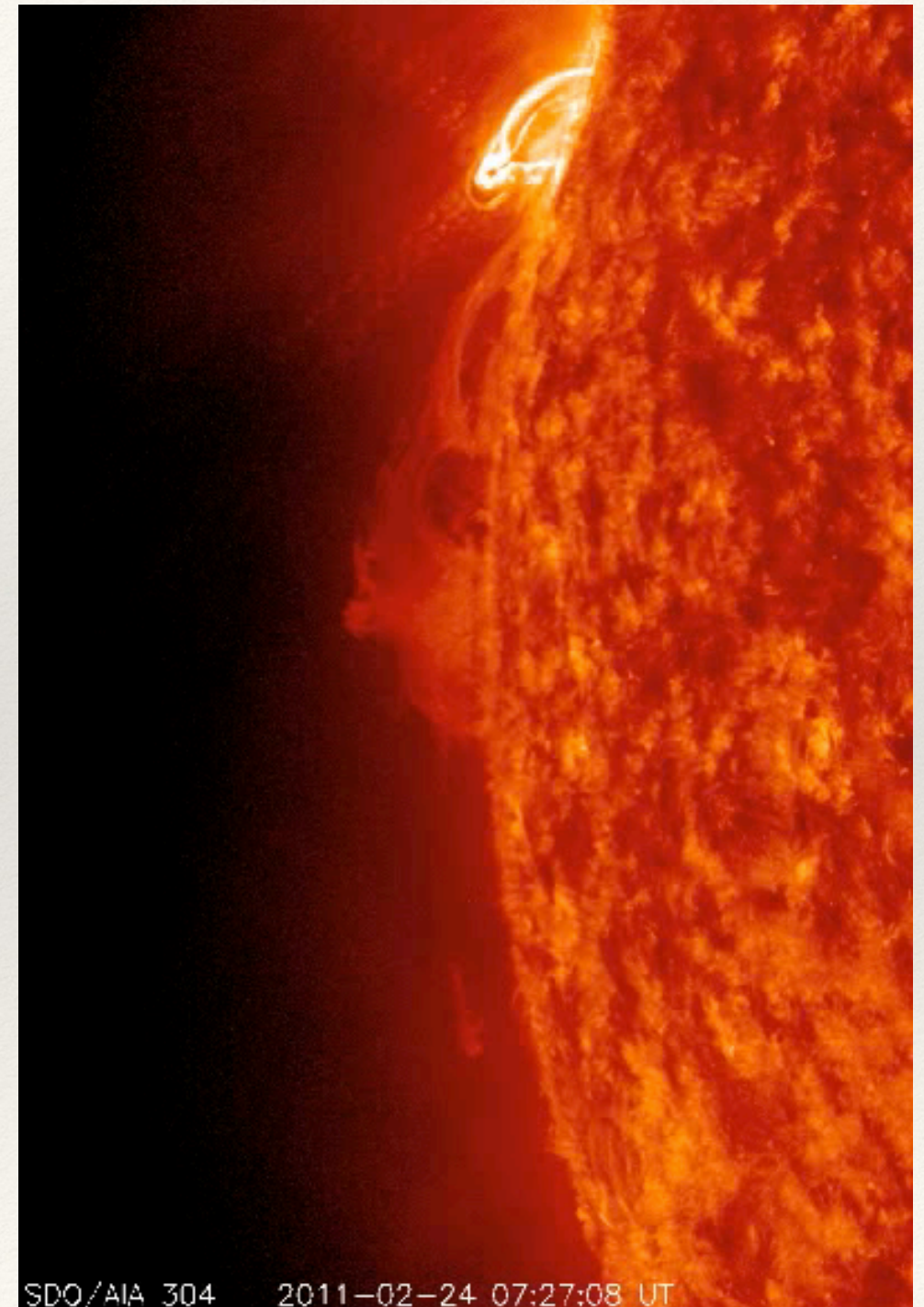
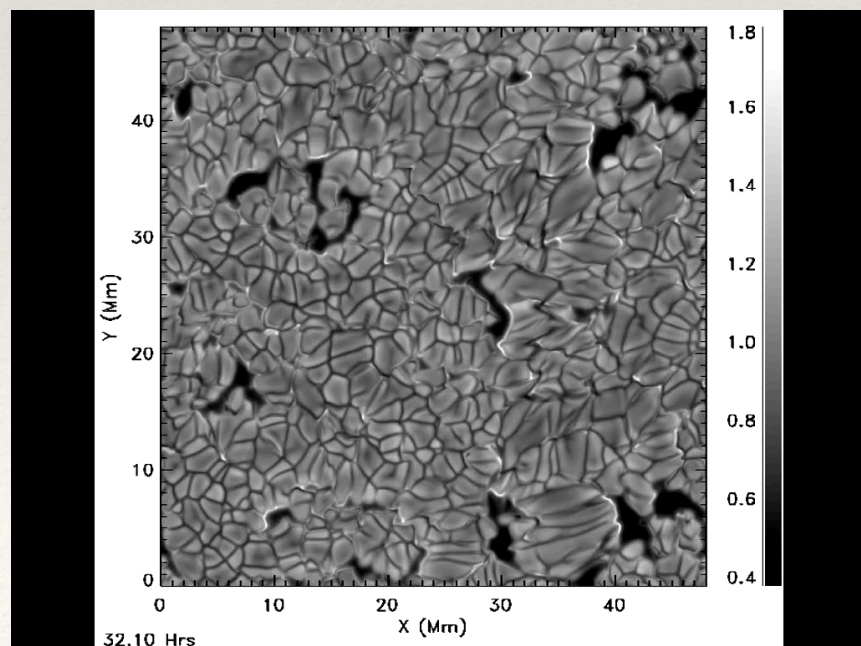
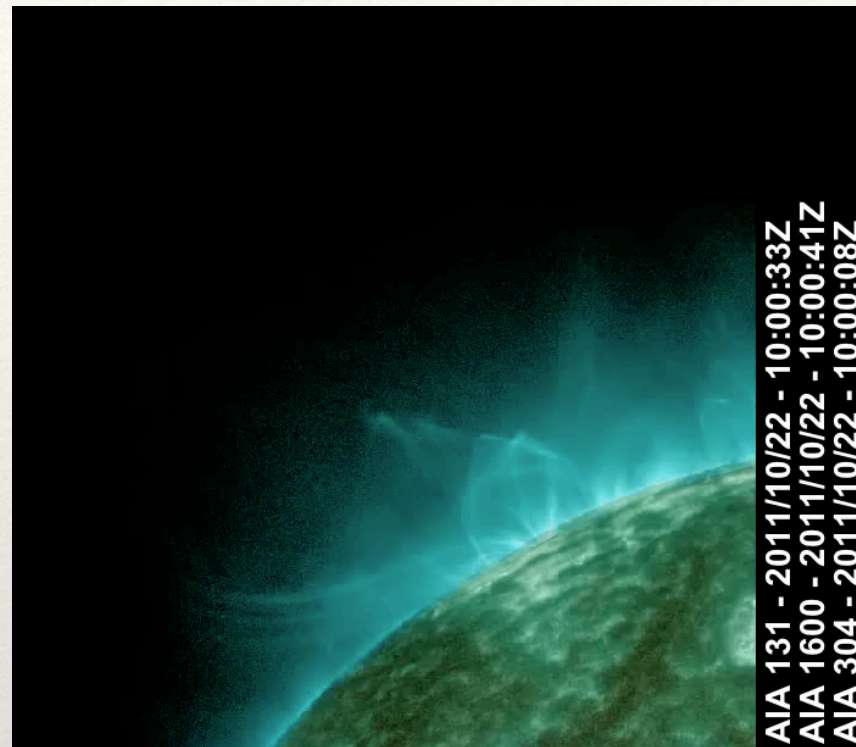


# Solar Dynamics Observatory

SDO/AIA 193 Å  
Equi. Temp ~ 2.000.000 K

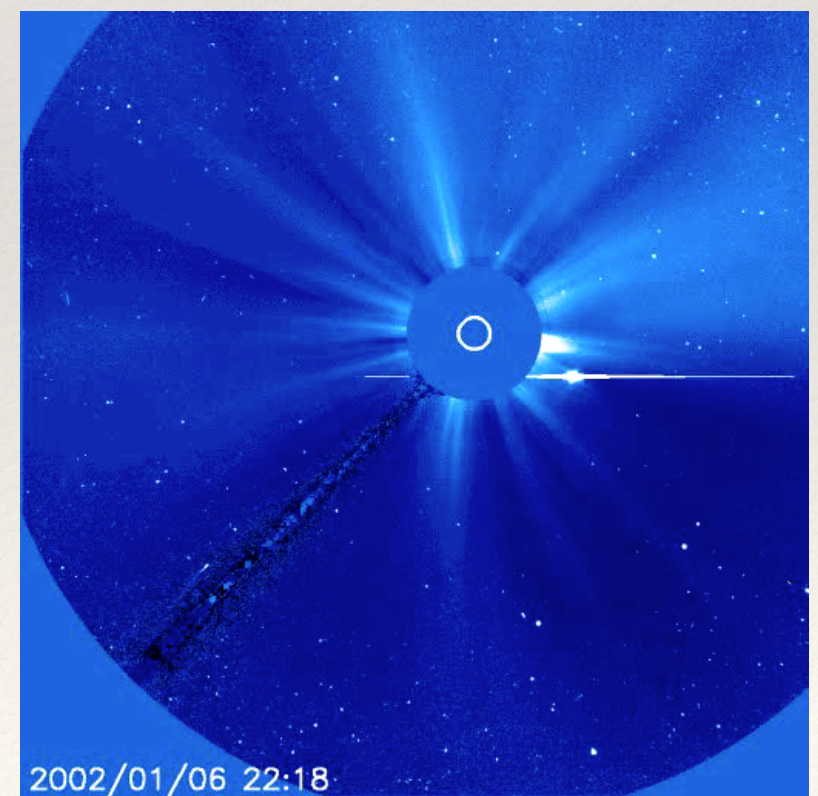
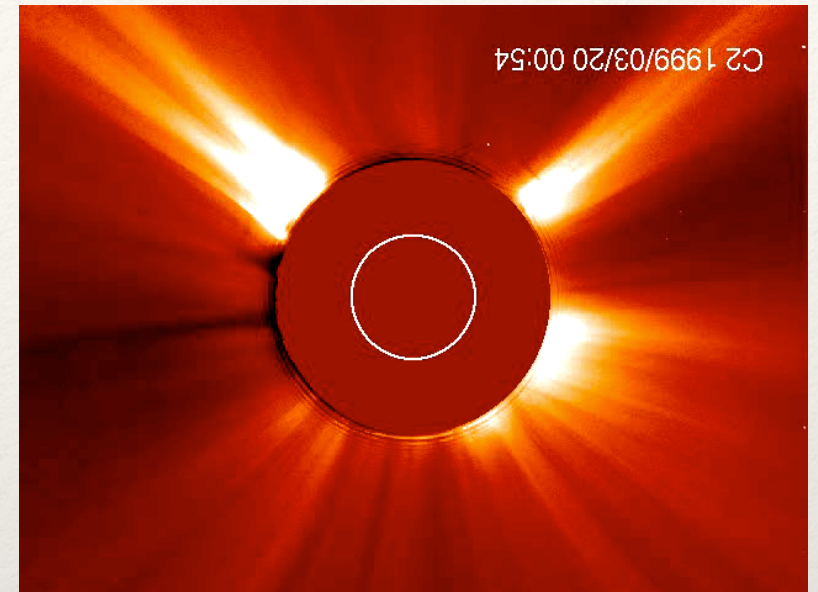
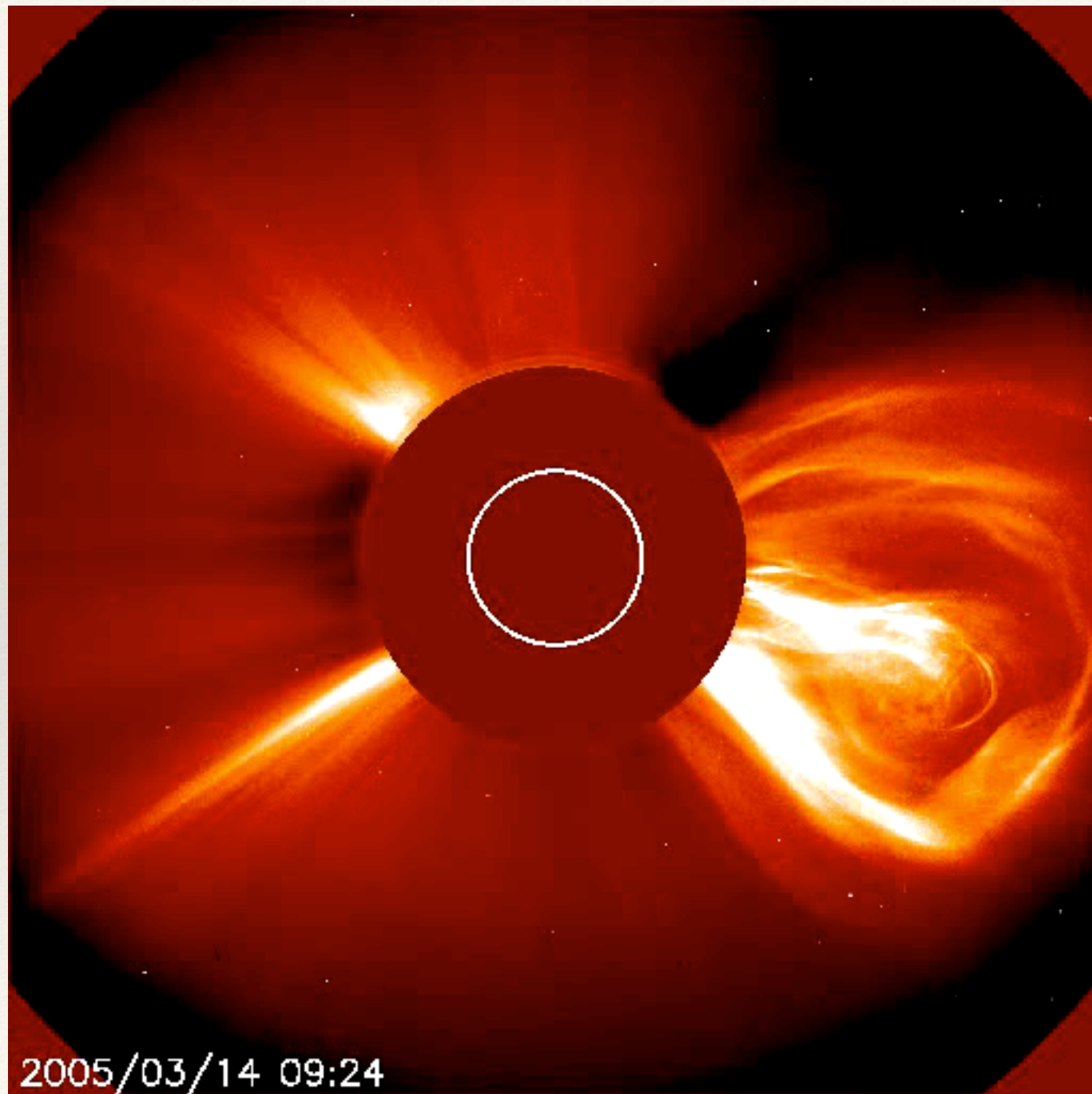


# A Solar Storm Launches



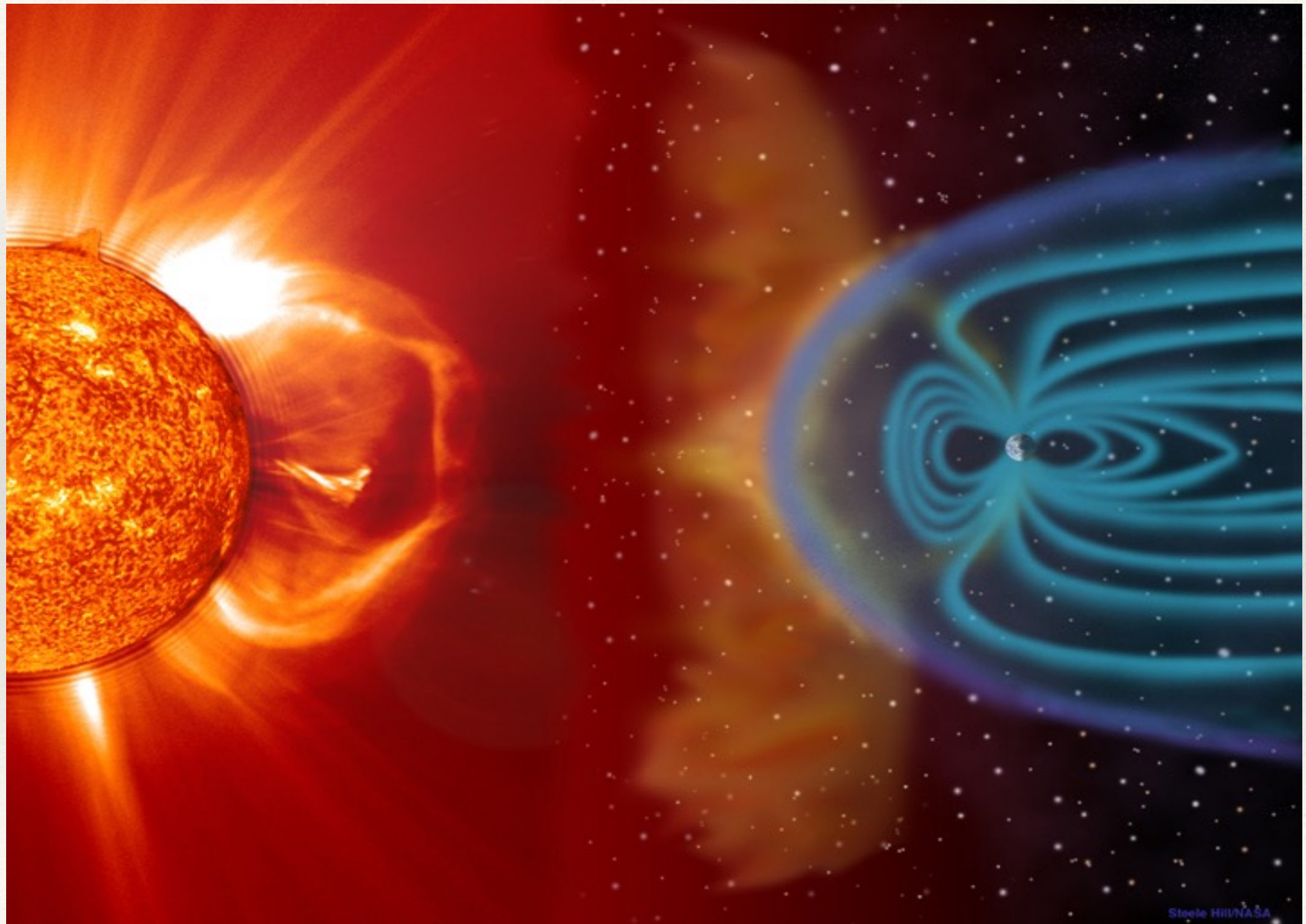


# The Solar Wind and the Storm





# The Sun-Earth Plasma Connection

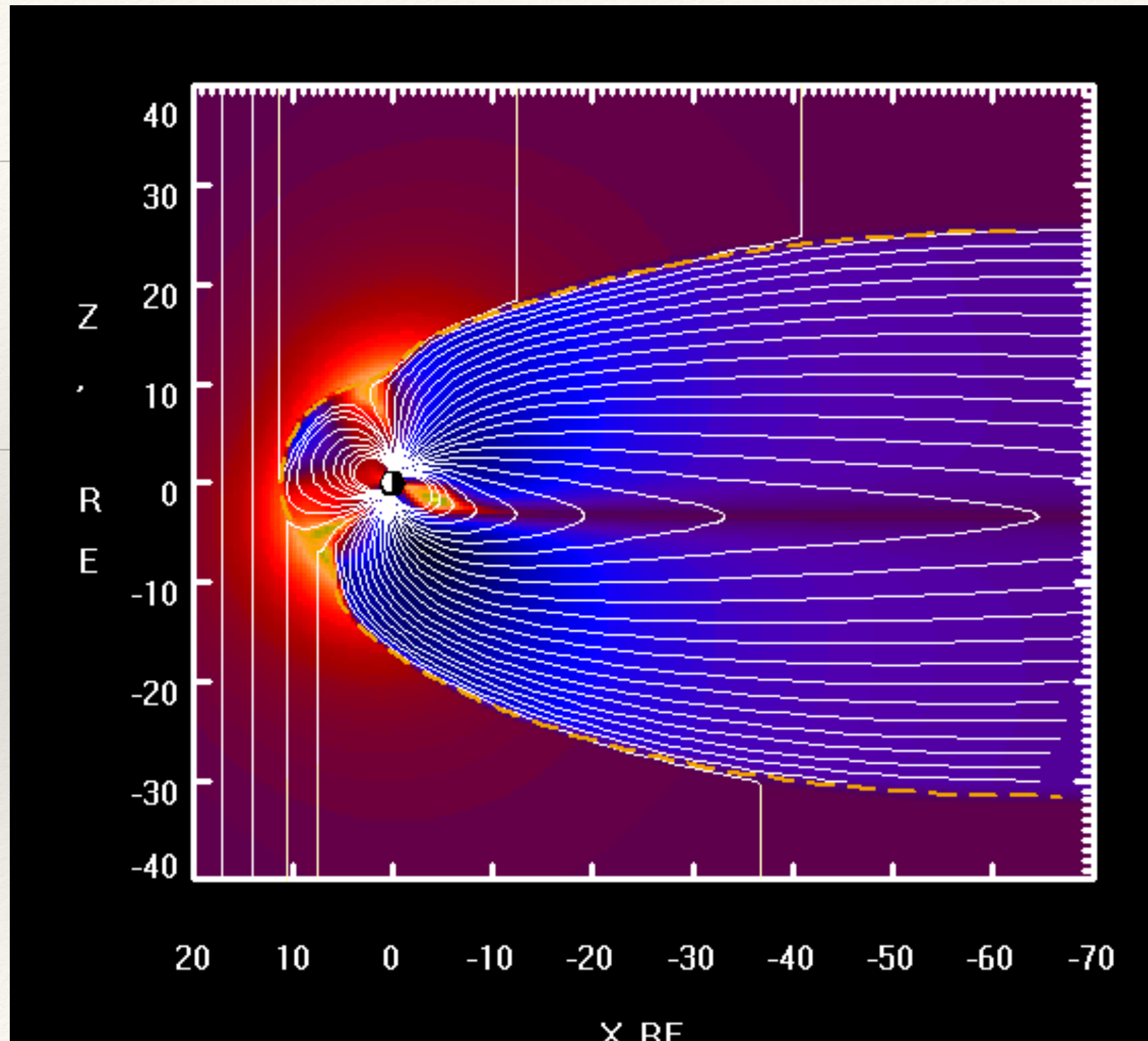




*Blowin' in The Wind*

# Geomagnetic Storms

Disruptions in the  
magneto-tail lead to  
strong currents and  
inductive magnetic  
fields on Earth

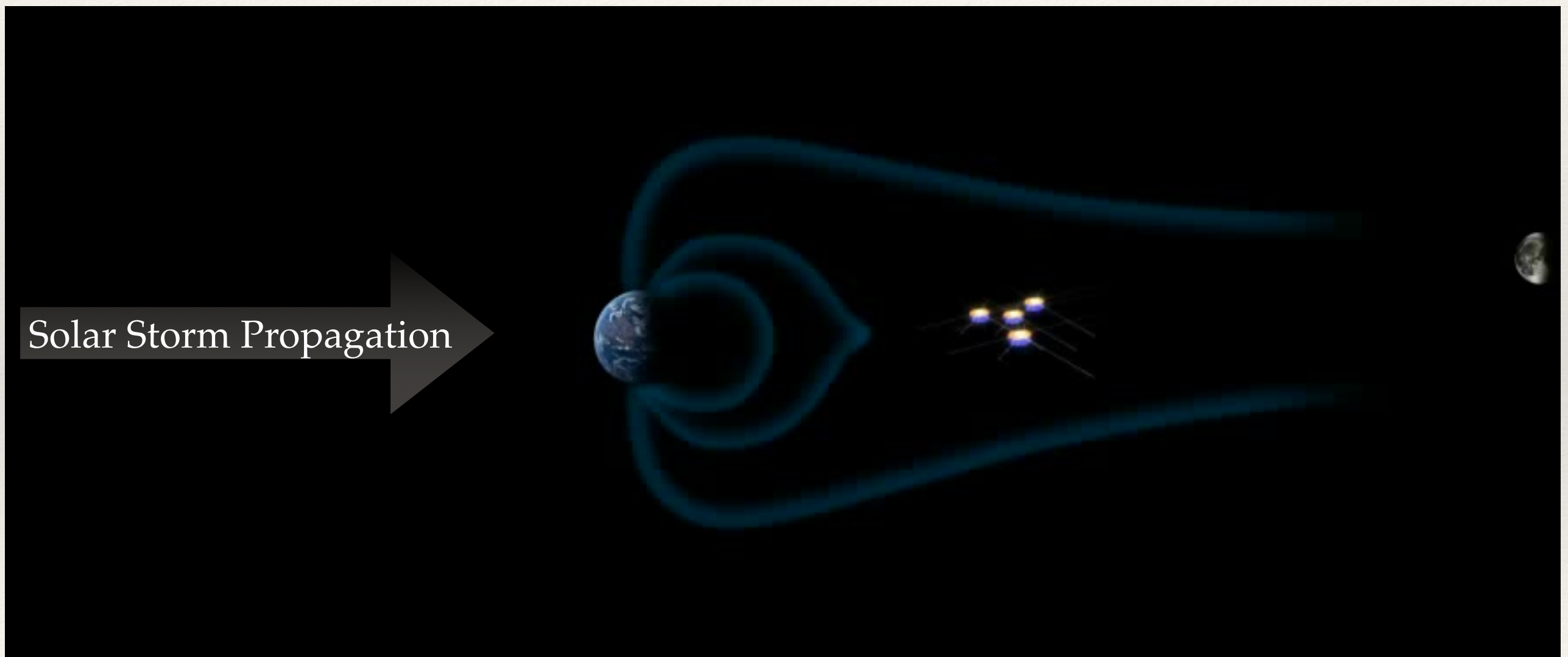




---

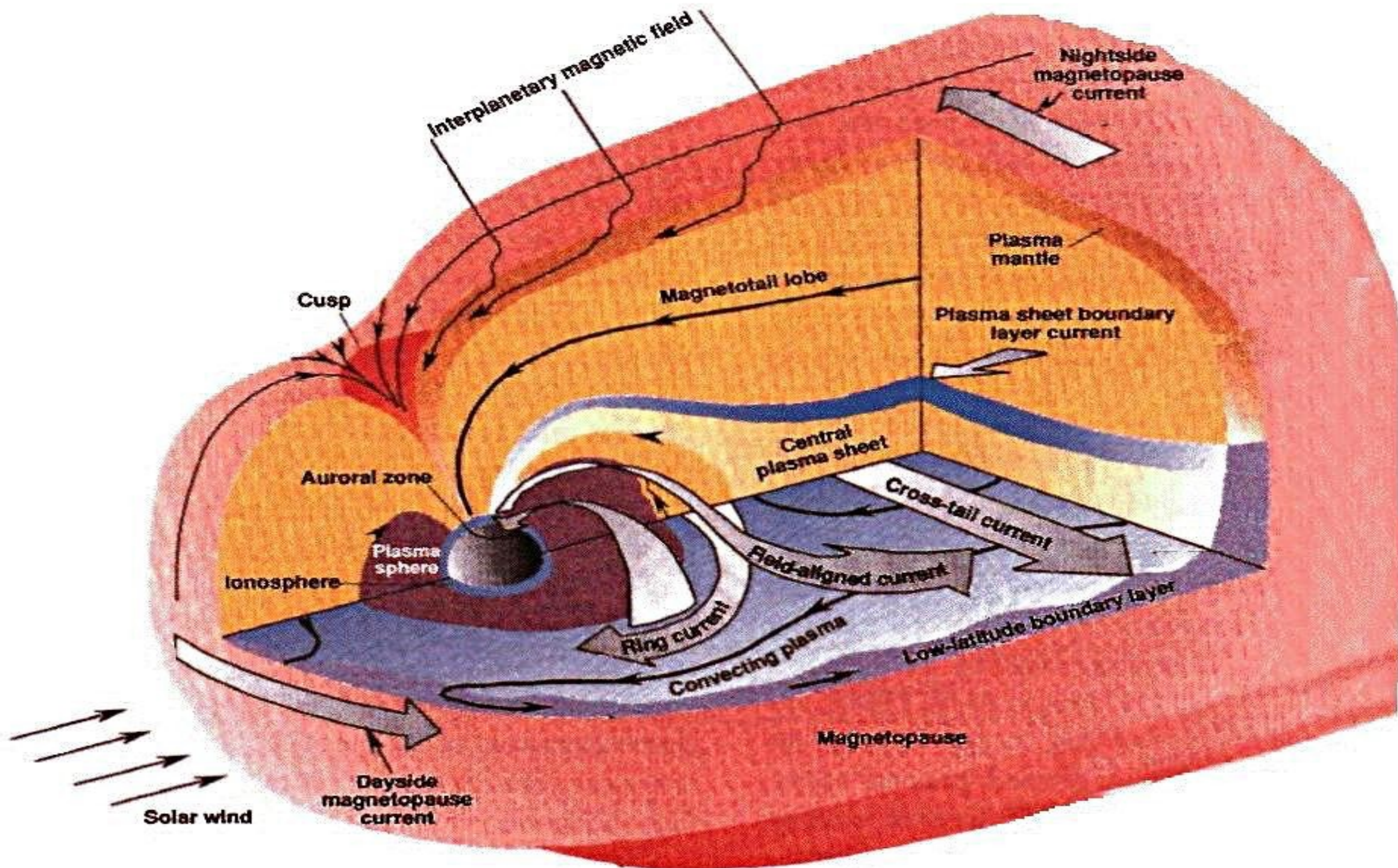
# CLUSTER Satellites 'see' Electro-jet During Solar Storm

---





# Earth's Complicated Current Systems

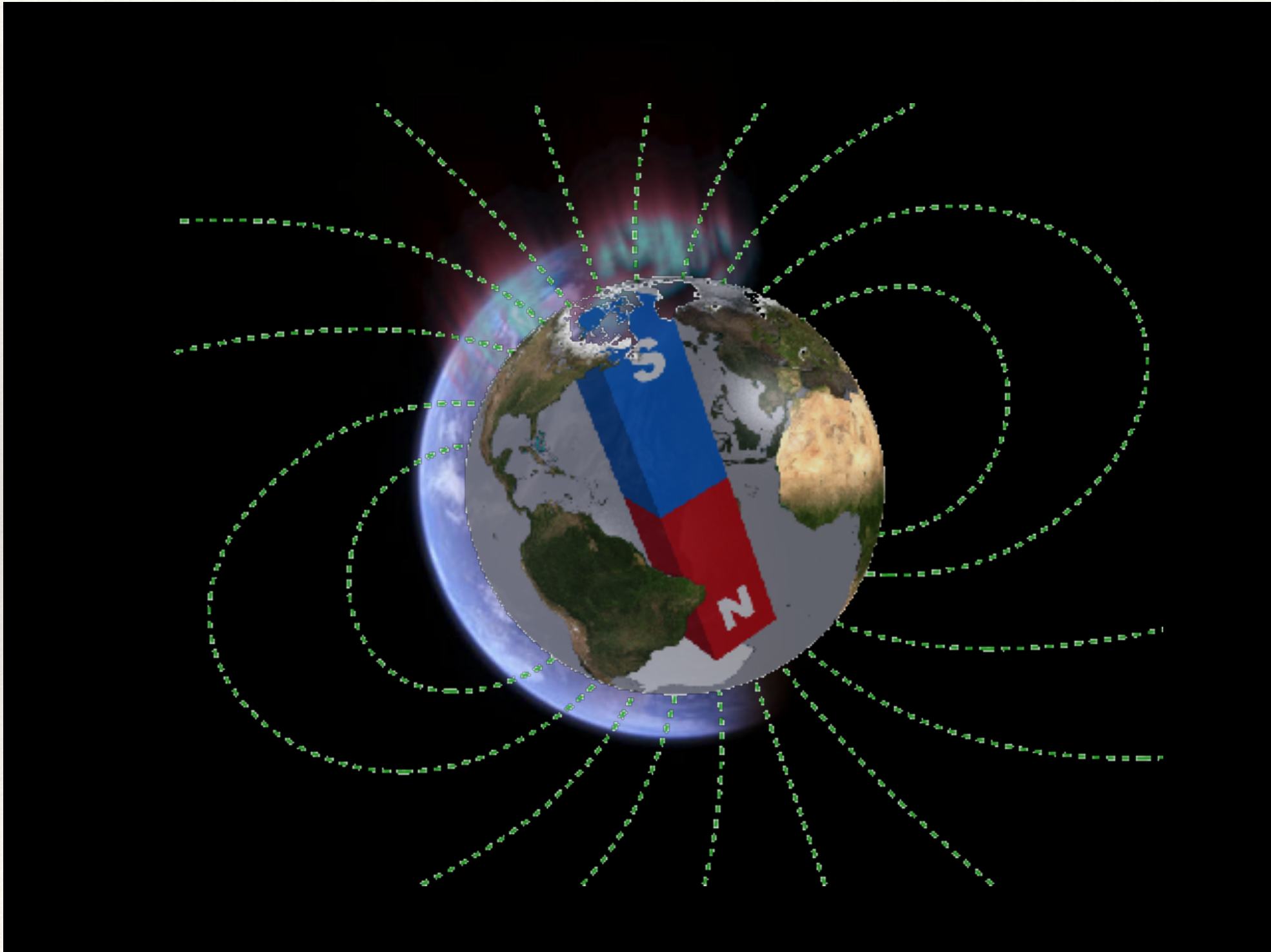




---

# Where Will Solar Storms Go?

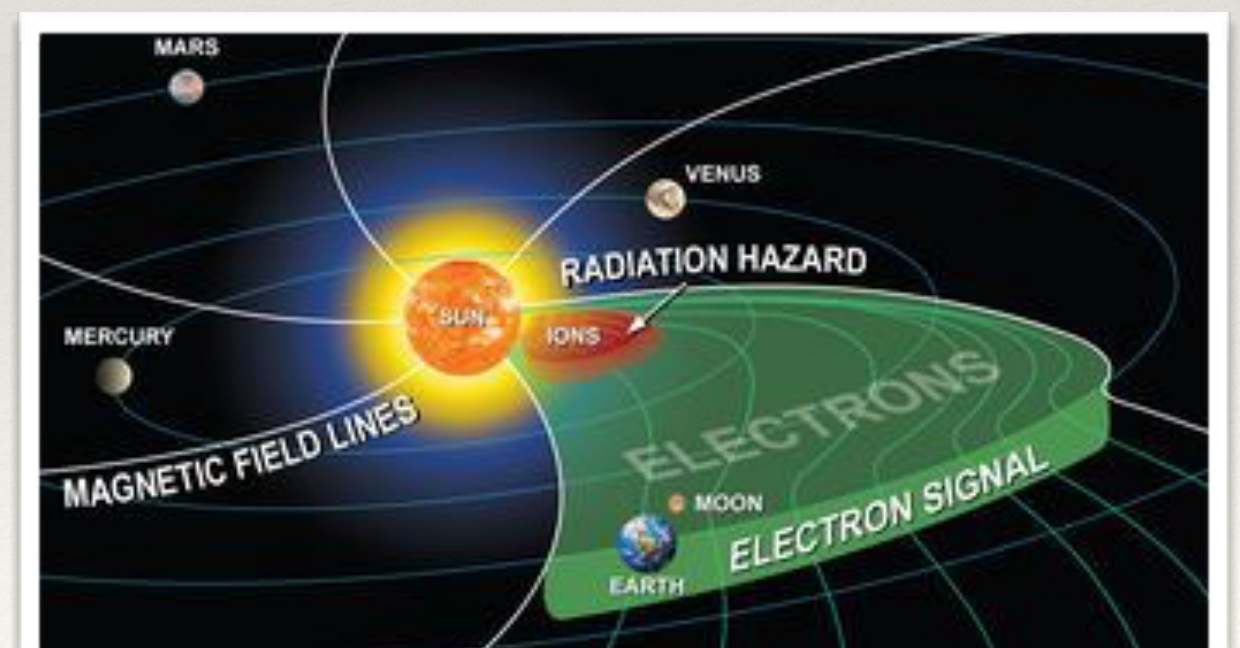
---





# Some Effects of Solar Storms

- ❖ Aurora Borealis
- ❖ Satellite Damage
- ❖ Power grid fall-out
- ❖ Pipelining at risk
- ❖ Data loss - or delay
- ❖ Radiation hazard for spaceborne mission





# Example, Quebec 1989

- Power grid fall-out i largest part of Quebec Province
- Aurorae observed in Texas, latitude about as Morocco!

Transformer coil of Quebec powerplant, post '89 storm,





---

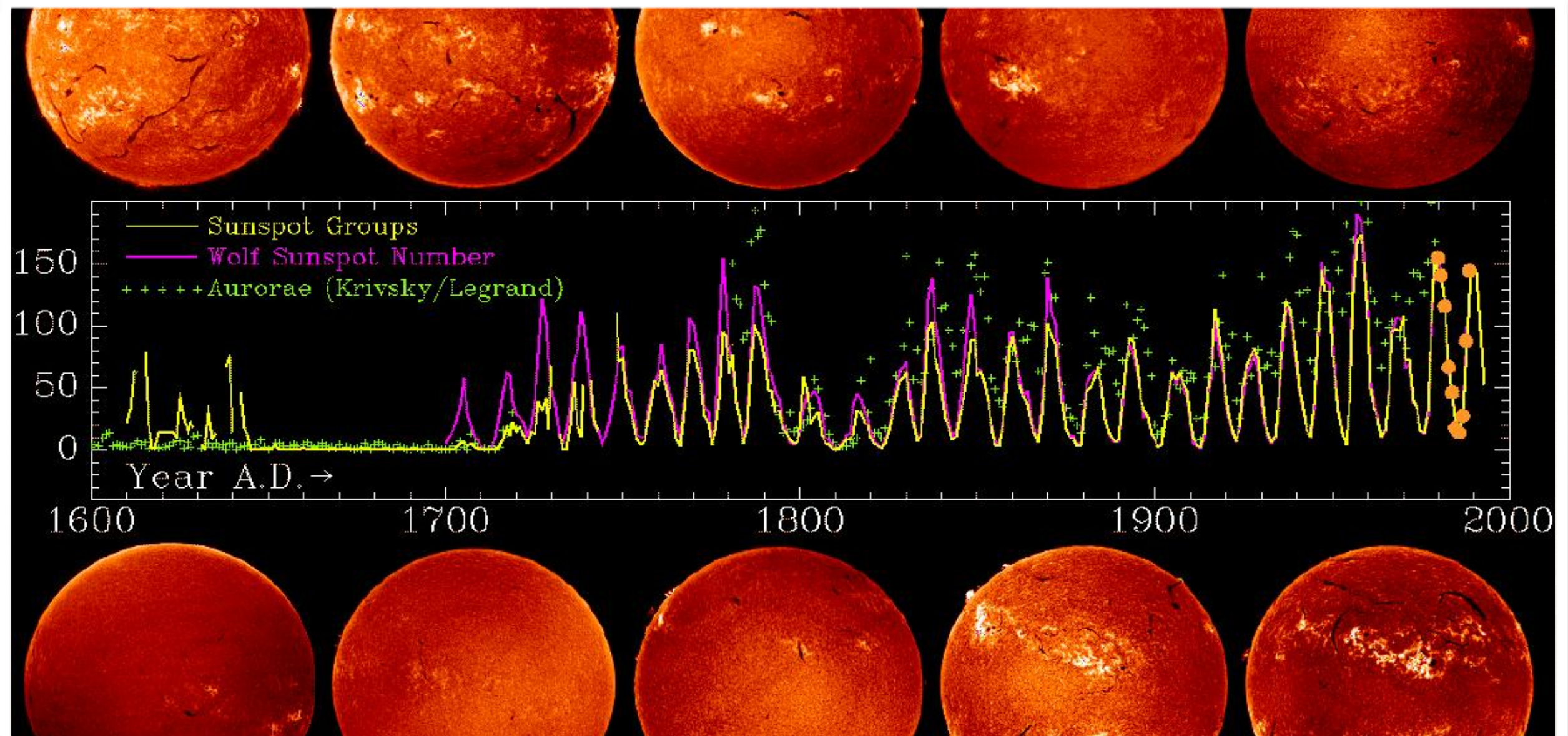
# Aurorae Seen From the ISS

---



Credit ISS crew / NASA, sept.17, 2011. Timelapsed movie from 12:22-12:45.





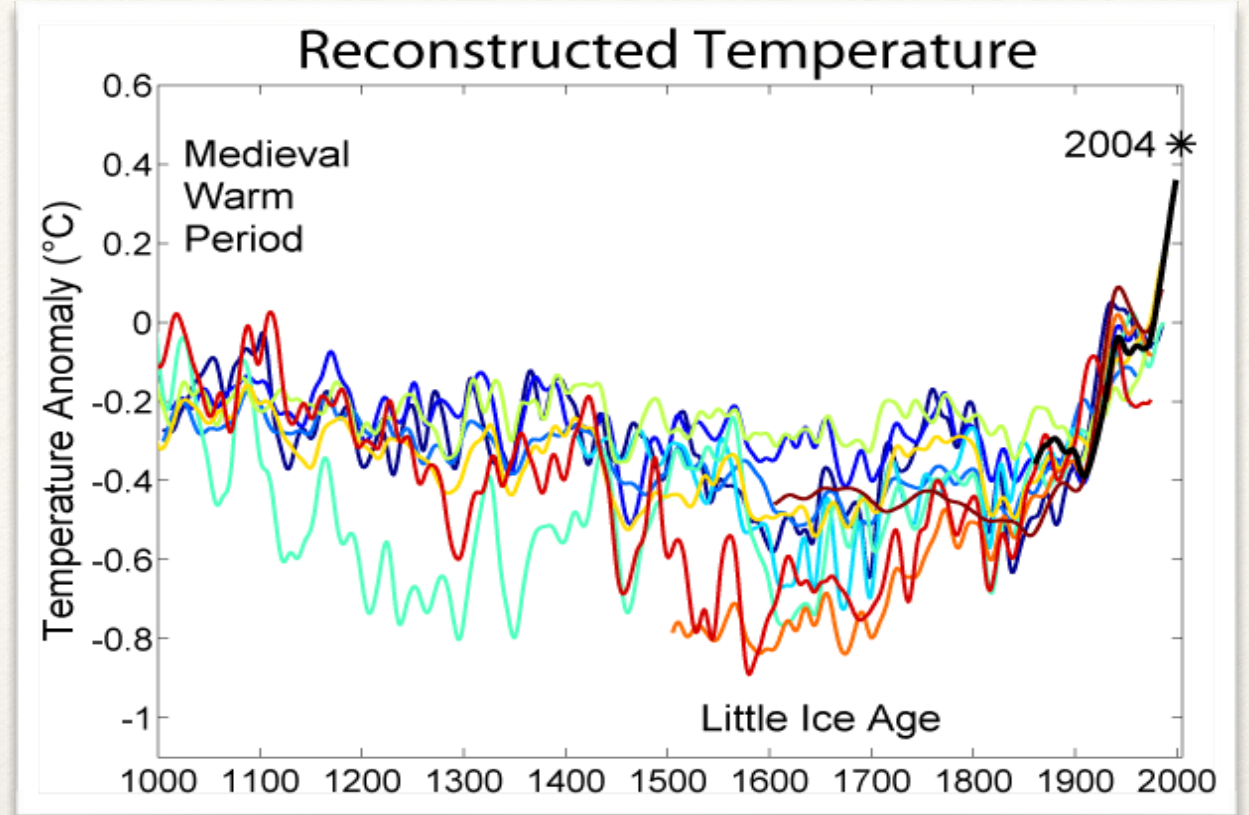
*Historical Sunspot Data: almost 400 years of “useless” counting.*

# Climate Questions...

Interesting perspectives

Does the solar cycle influence Earth in usual ways?



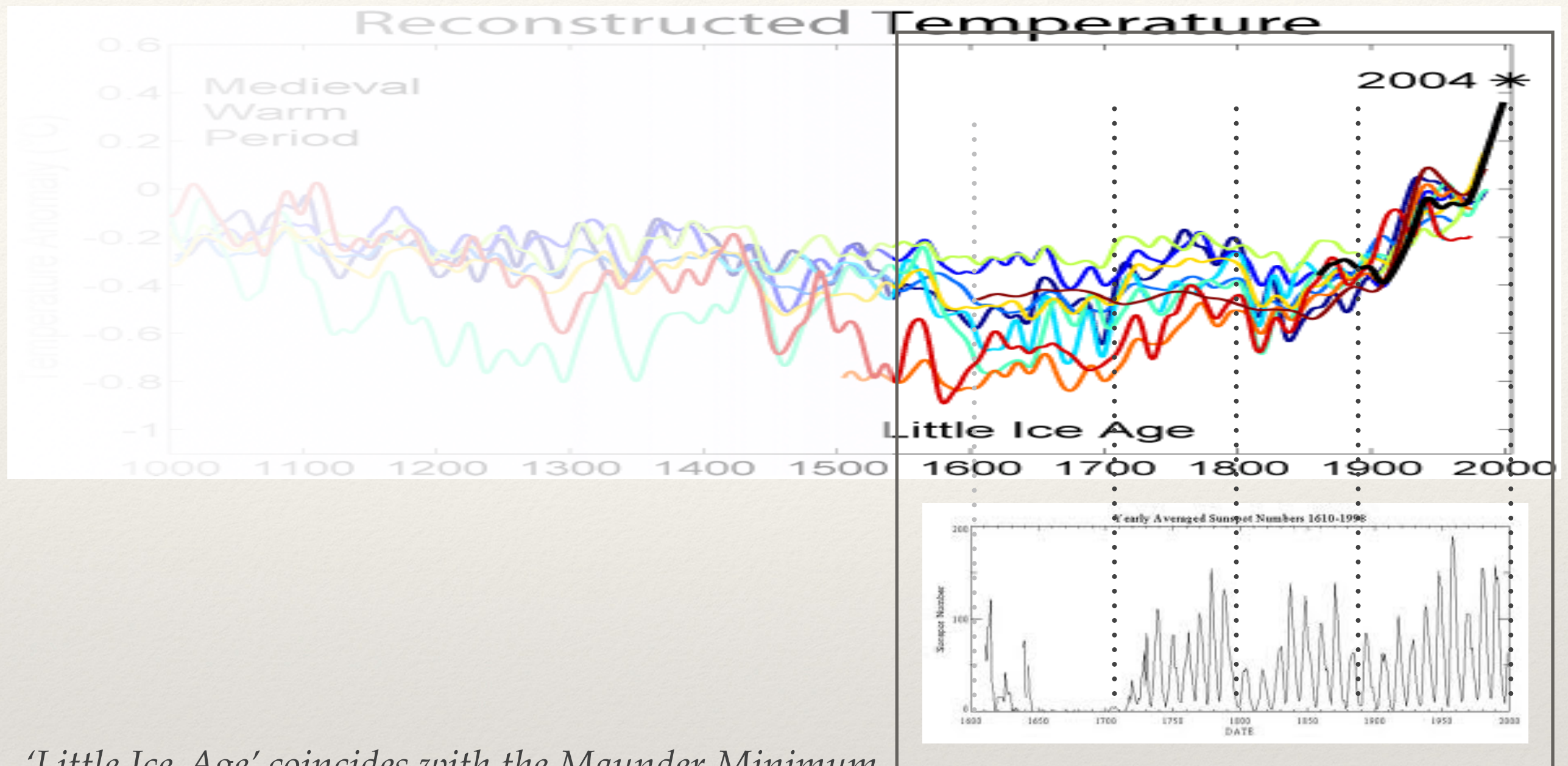


*'Little Ice-Age' coincides with the Maunder Minimum*

# Climate Questions...

A coincidence?  
Perhaps.



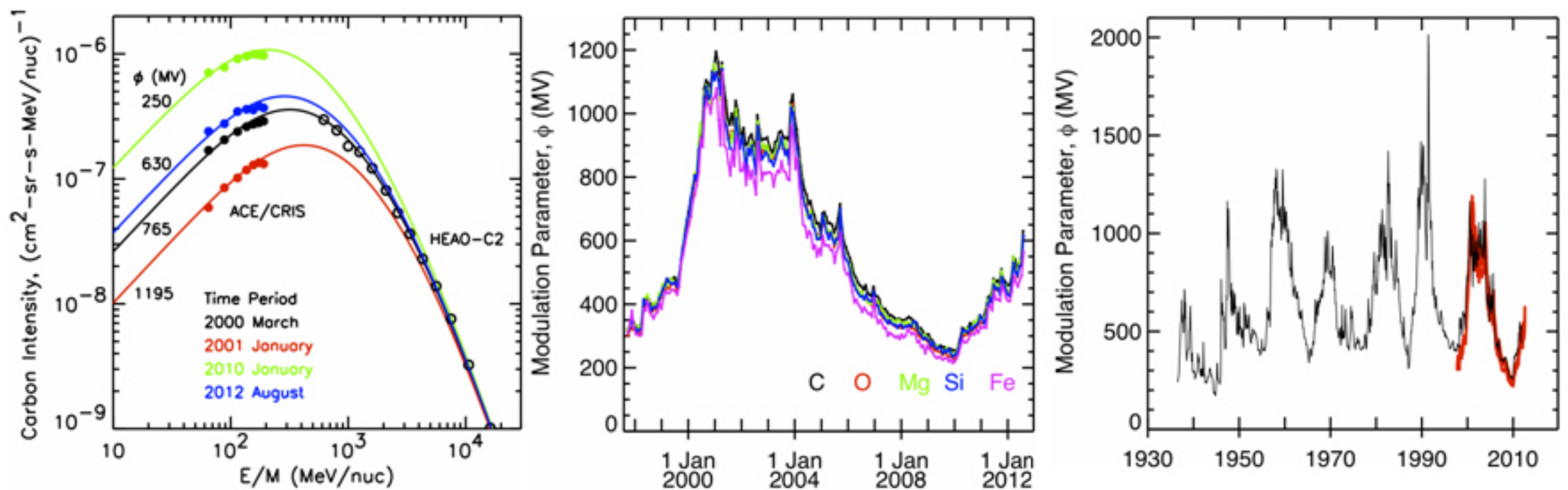


*'Little Ice-Age' coincides with the Maunder Minimum*

# Climate Questions...

A coincidence?  
Perhaps.





## *Solar Modulation of Cosmic Ray Spectrum*

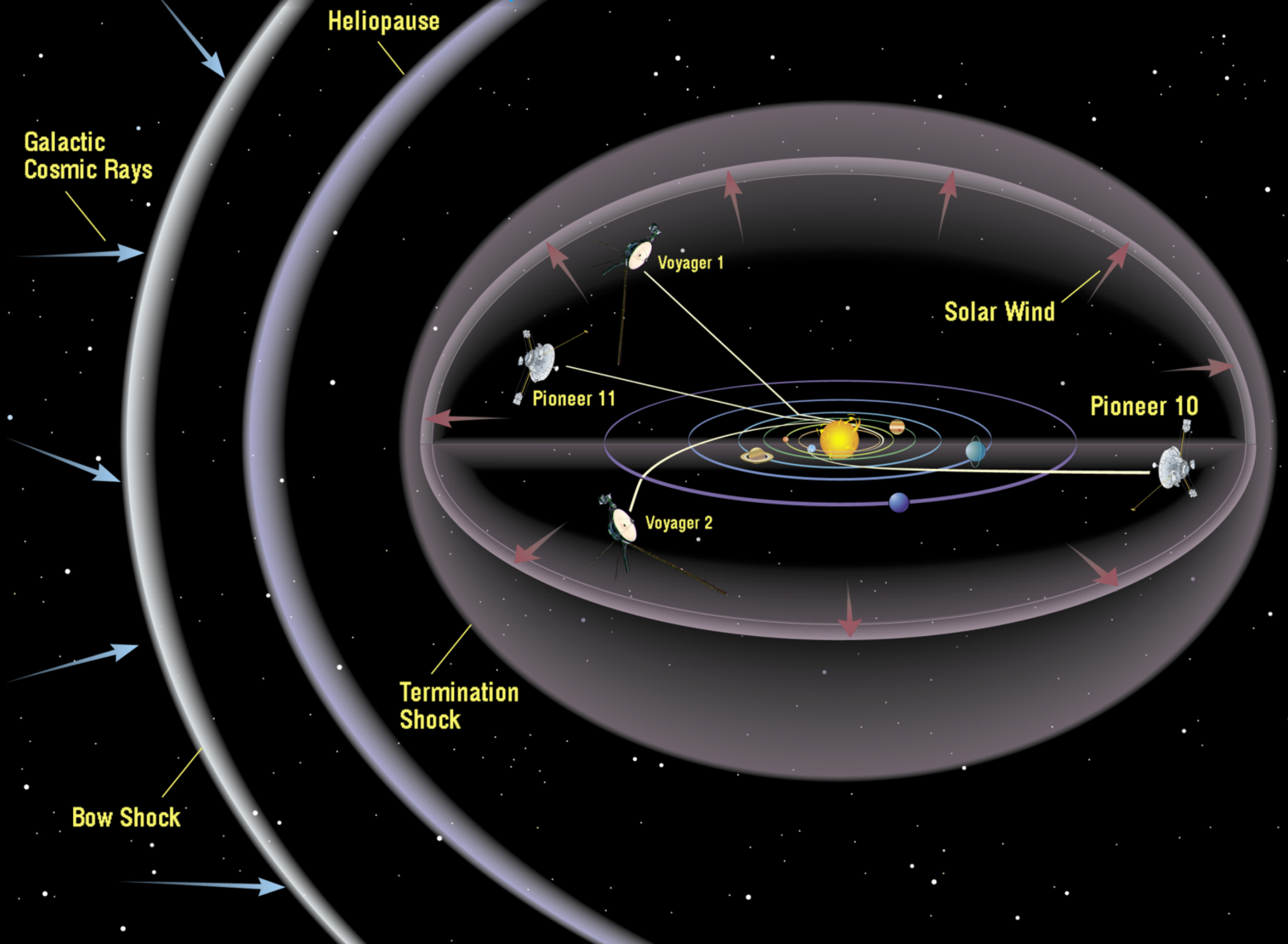
# Climate Questions...

The Cosmic Ray Spectrum is correlated with the solar cycle.

More active Sun?  
Less cosmic rays.



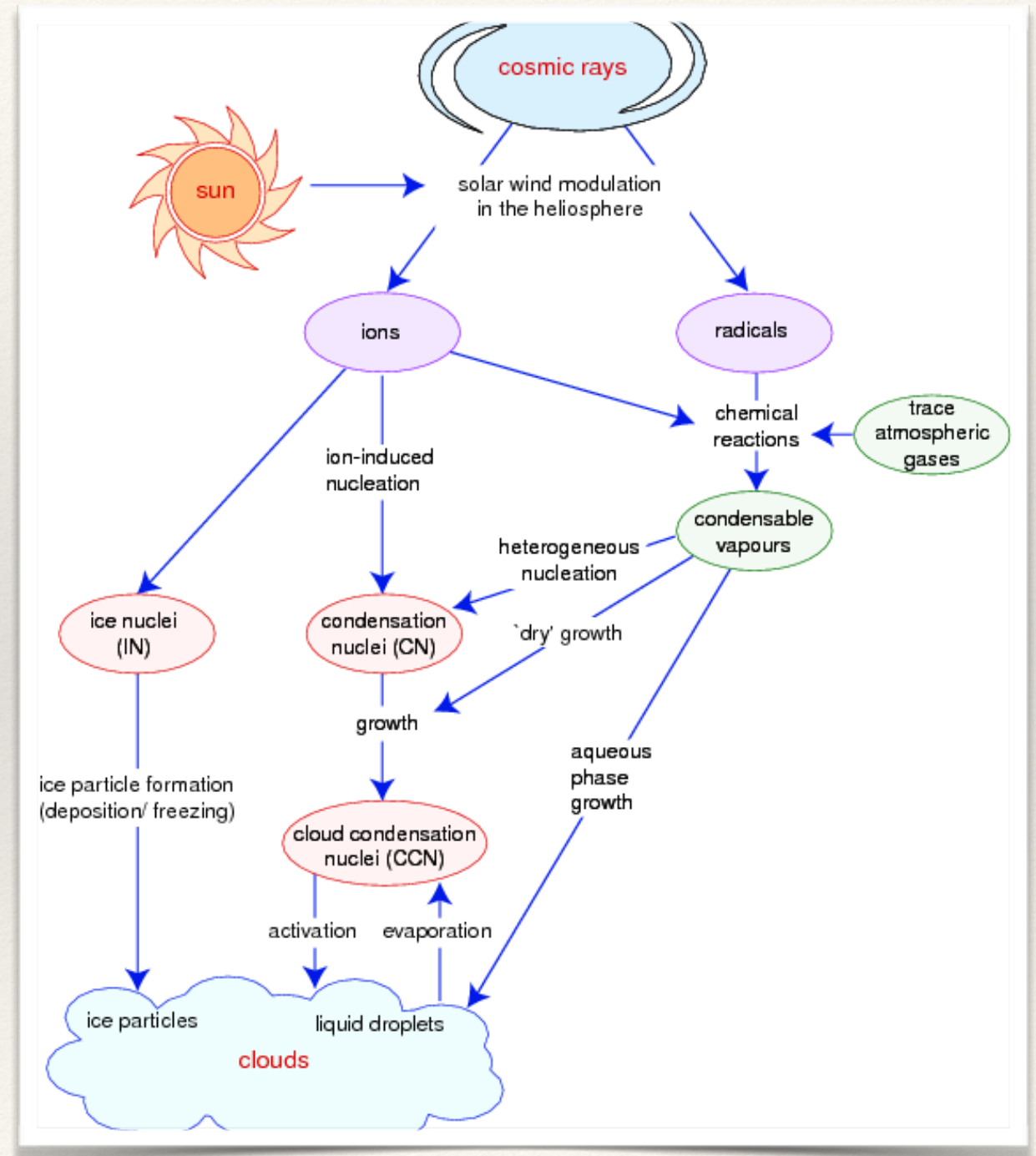
The magnetized heliosphere shields the solar system, and Earth





# Climate Questions... end?

- ❖ Cloud nucleation by cosmic rays?
- ❖ Cloud formation?
- ❖ Would influence global cloud coverage.
- ❖ Thence, global temperatures.
- ❖ Effect, if any, most likely benign.
- ❖ Not verified, in some cases even contradicted by simulations.
- ❖ However not falsified totally either.
- ❖ Yet a long way to go, as for clouds in general.





“Gimme’ a break — Please.”

*[10 minutes]*



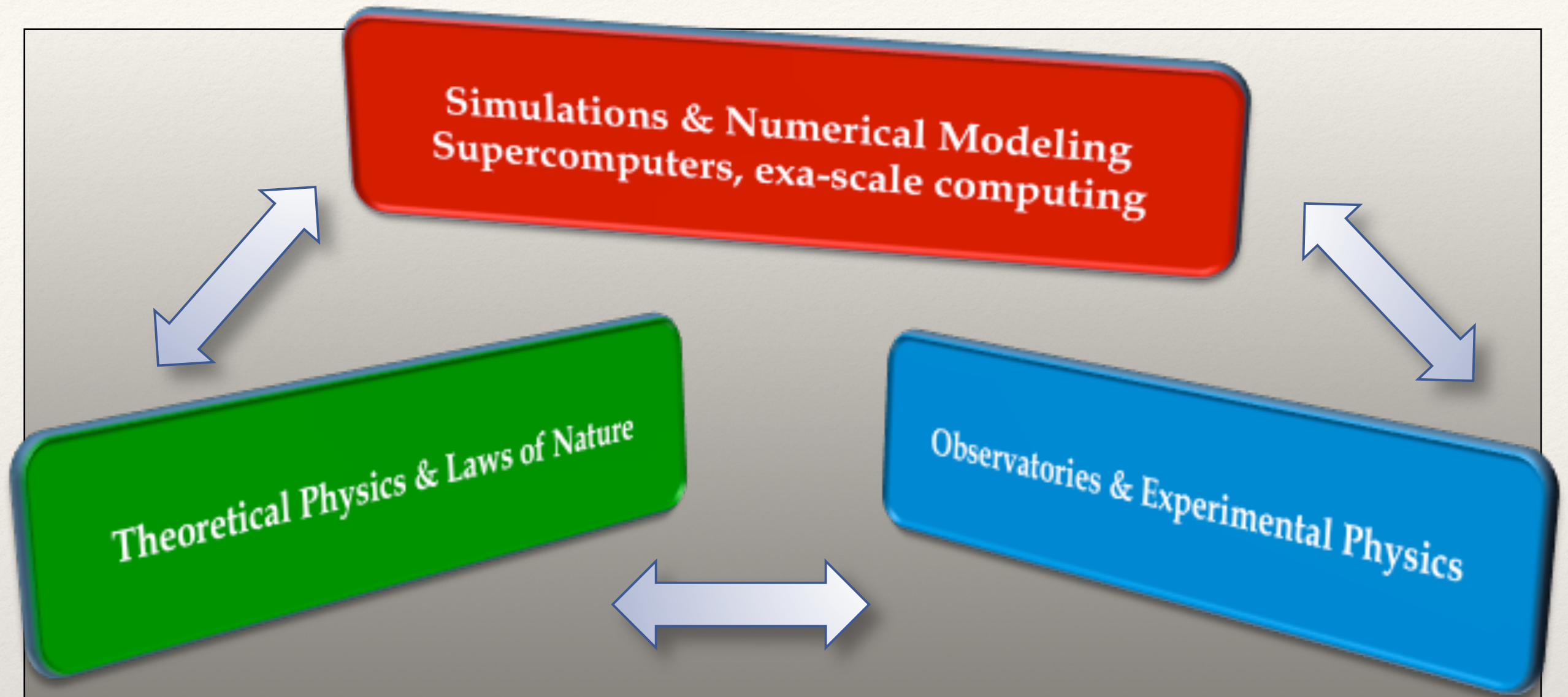
*Solar Storms, Revisited & Modelled*

---

# Part III

- A Third Branch in Science
  - Computational Modeling
  - Detailed Numerical Studies of a Flaring Active Region
-





*From Two to Three Players in Science*

# Computational (Astro)physics

- Exa-scale Computing offers:
  - $10^{18}$  FLOPS
  - $10^{18}$  Bytes
- A Realistic Player When Investigating Hypotheses
- Eventually Even Predictive

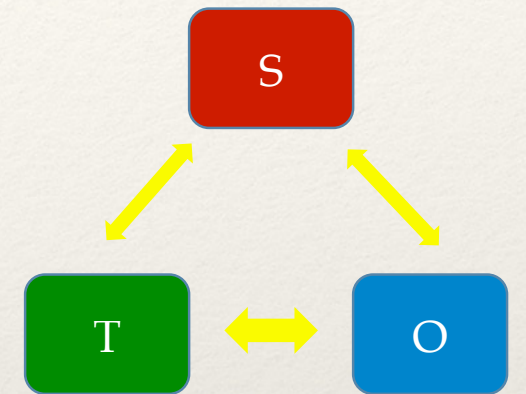


---

# The Sun provides an Excellent “Laboratory” for this ‘Triad of Science’

---

- ❖ From theory we get the fundamental equations and Laws of Nature to tell us what to look for.
- ❖ From observations we get data to feed modelers.
- ❖ From simulations we get results that can test hypotheses.
- ❖ Detailed simulations can even yield predictive results(!)



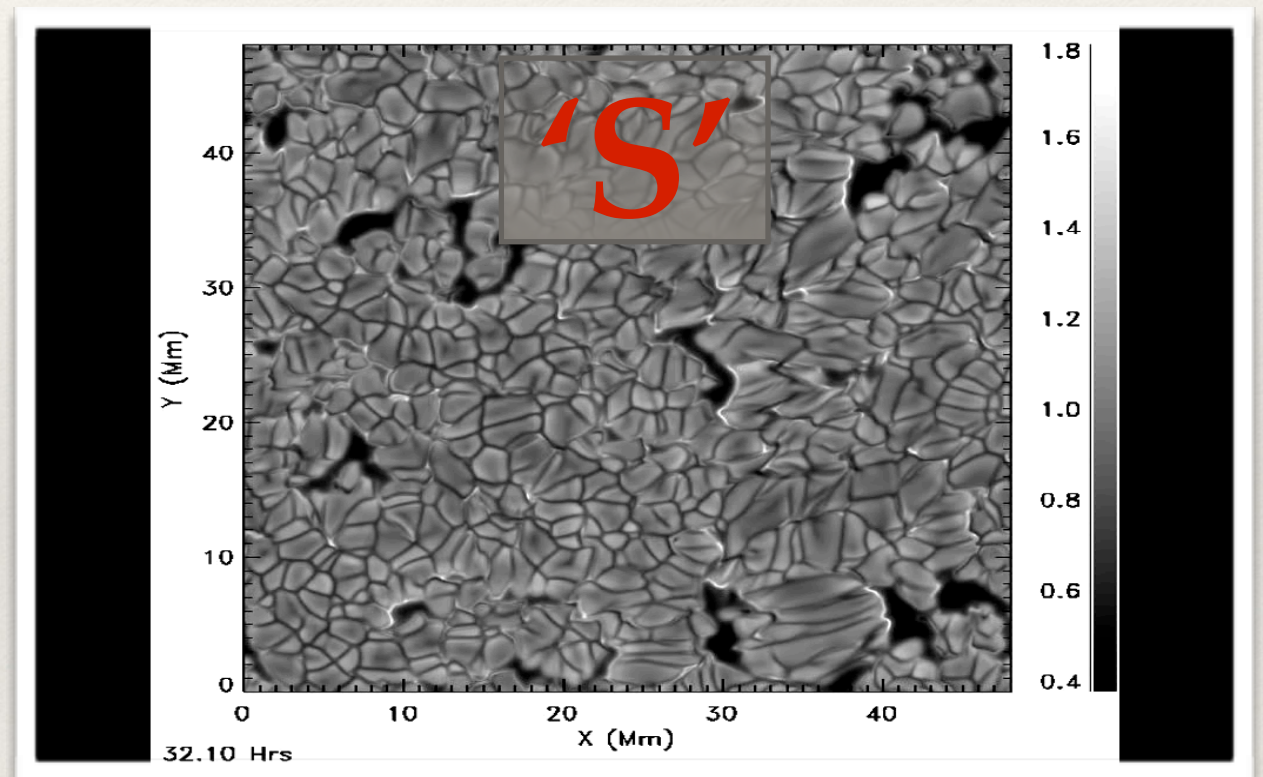


# The Sun as a “Laboratory”

*Example of verification & adjustment of computer simulations.*



2 days of photospheric footage. The Solar Dynamics Observatory “white” light ( $\sim 5200\text{K}$ ).

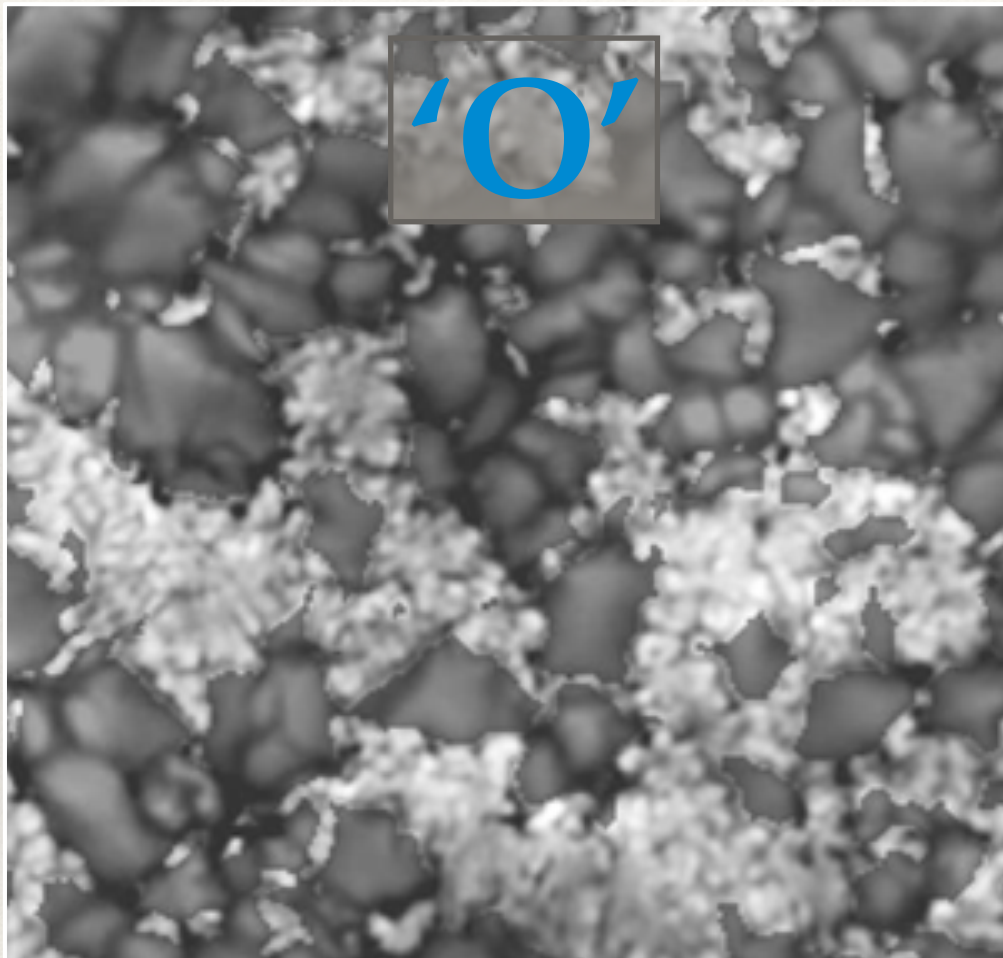


2 days of photospheric footage. The Stagger Code (NBI) in “white” light ( $\sim 5200\text{K}$ ).

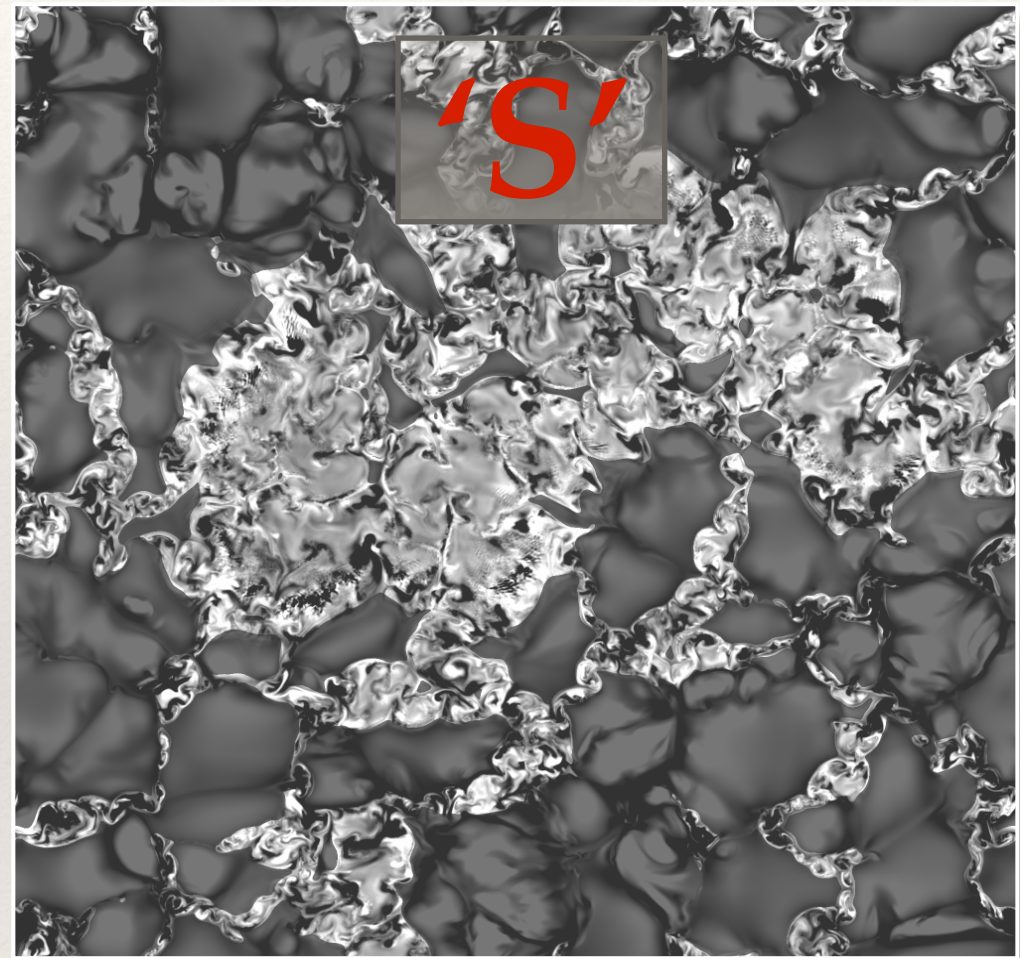


# The Sun as a “Laboratory”

*Example of “predictive” power of computer simulations.*



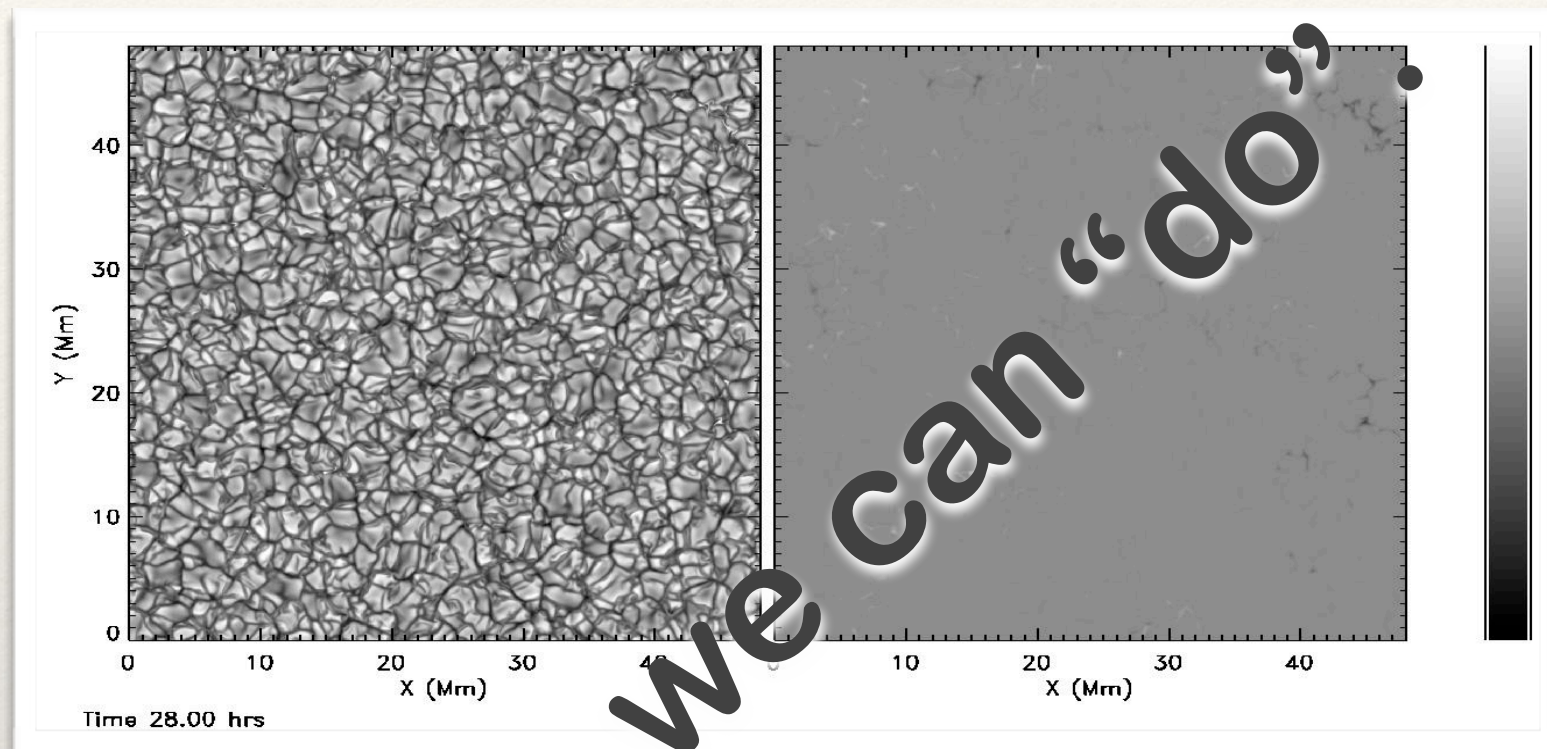
Credit: Swedish 1-m Solar Telescope  
Narayan & Scharmer (2010)



Credit: “Active region magneto-convection”  
Nordlund *et al.*, NBI/Cph (~2010)

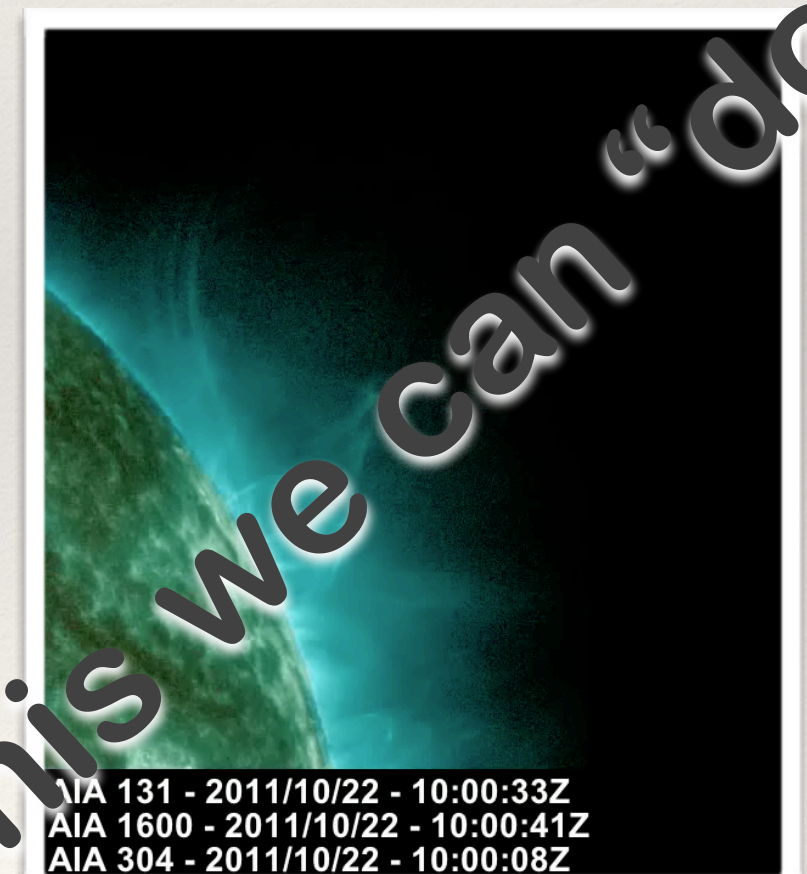


# Essentials of Solar Storm Initiation



- ❖ Deep photospheric convection
- ❖ Transport of magnetic flux
- ❖ Magnetic flux emergence

- ❖ Photospheric driving stress-energy into Coronal magnetic field
- ❖ Release of magnetic stress-energy and Coronal heating.





# Essentials of Solar Storm Initiation

- ❖ Explosive relaxation of stress-energy
- ❖ Flaring
- ❖ Realistic coronal mass ejections — CMEs
- ❖ Solar energetic particle events — SEPs





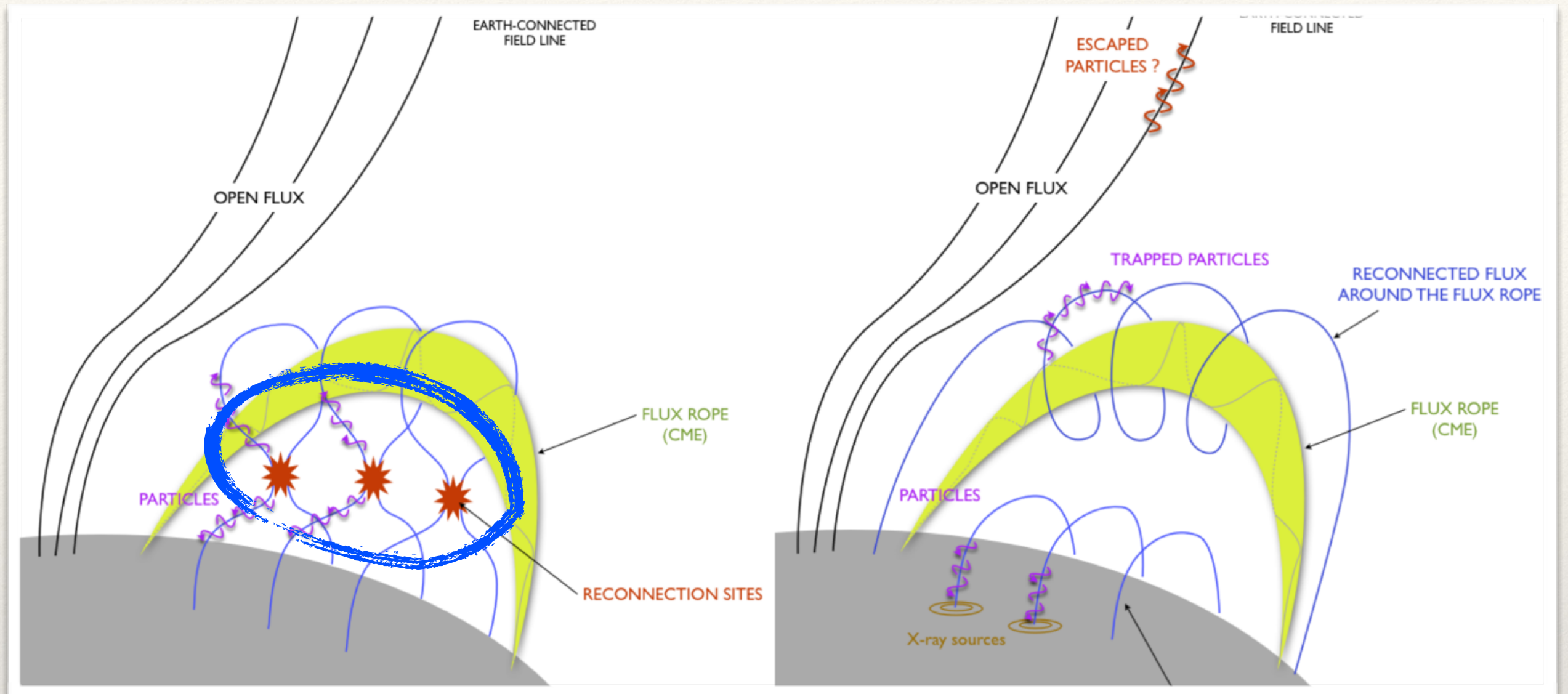
*Solving a Puzzle? — The Road Ahead*

---

# Part IV

- A ‘generic’ solar storm configuration
  - The “puzzle” of Magnetic Reconnection
  - Numerical plasma physics, today.
  - Numerical plasma physics, tomorrow?
-





Lorem Ipsum Dolor

# A 'Generic' Solar Storm Configuration

- Flux rope becomes buoyant and lifts into the Corona.
- Magnetic Reconnection sets in.
- Flux rope explosively lifts into interplanetary MF.



# The “Puzzle” of Magnetic Reconnection (MR)

The fully kinetic plasma description — we already saw this, remember? :-)

$$\left. \frac{\partial f^i}{\partial t} + \mathbf{u} \cdot \frac{\partial f^i}{\partial \mathbf{x}} + \frac{q^i}{m^i} (\mathbf{E} + \mathbf{u}_i \times \mathbf{B}) \cdot \frac{\partial f^i}{\partial (\mathbf{u}\gamma)^i} = \frac{\partial f^i}{\partial t} \Big|_{coll} \right\} \text{Vlasov-Boltzmann}$$

$$\left. \begin{aligned} -\frac{\partial \mathbf{B}}{\partial t} &= \nabla \times \mathbf{E} \\ \frac{1}{c^2} \frac{\partial \mathbf{E}}{\partial t} &= \nabla \times \mathbf{B} - \mu_0 \mathbf{J} \end{aligned} \quad \begin{aligned} \nabla \cdot \mathbf{E} &= \frac{\rho_c}{\epsilon_0} \\ \nabla \cdot \mathbf{B} &= 0 \end{aligned} \right\} \text{Maxwell}$$

$$\left. \begin{aligned} \rho_c(\mathbf{x}) &= \int d\mathbf{u} \sum_i q^i f^i(\mathbf{x}, \mathbf{u}) \\ \mathbf{J}(\mathbf{x}) &= \int d\mathbf{u} \sum_i \mathbf{u} q^i f^i(\mathbf{x}, \mathbf{u}) \end{aligned} \right\} \text{EM Sources}$$



# The “Puzzle” of Magnetic Reconnection (MR)

The Magneto-Hydrodynamic approximation ‘MHD’ — a single magnetized fluid

$$\frac{\partial \rho}{\partial t} + \nabla \cdot (\rho \mathbf{v}) = 0$$

$$\nabla \cdot \mathbf{B} = 0$$

$$\rho \left( \frac{\partial}{\partial t} + \mathbf{v} \cdot \nabla \right) \mathbf{v} = \mathbf{J} \times \mathbf{B} - \nabla p$$

$$\frac{\partial \mathbf{B}}{\partial t} = -\nabla \times \mathbf{E}$$

$$\frac{d}{dt} \left( \frac{p}{\rho^\gamma} \right) = 0$$

$$\mathbf{E} + \mathbf{v} \times \mathbf{B} = 0$$

Ohm’s Law — no (low) resistivity  $\Rightarrow$  no magnetic diffusion!

$$\mu_0 \mathbf{J} = \nabla \times \mathbf{B}$$

Ampere’s Law — ‘slow(er)’ phenomena (no  $\frac{\partial \mathbf{E}}{\partial t}$  term)



# The “Puzzle” of Magnetic Reconnection (MR)

From MHD approximation

$$\frac{\partial \mathbf{B}}{\partial t} = \nabla \times (\mathbf{V} \times \mathbf{B}) + \frac{\eta_{res}}{\mu_0} \nabla^2 \mathbf{B}$$

Lundquist Number

$$S = \frac{\mu_0 V L}{\eta_{res}} \simeq \frac{|\nabla \times (\mathbf{V} \times \mathbf{B})|}{|(\eta/\mu_0) \nabla^2 \mathbf{B}|}$$

..... Advection

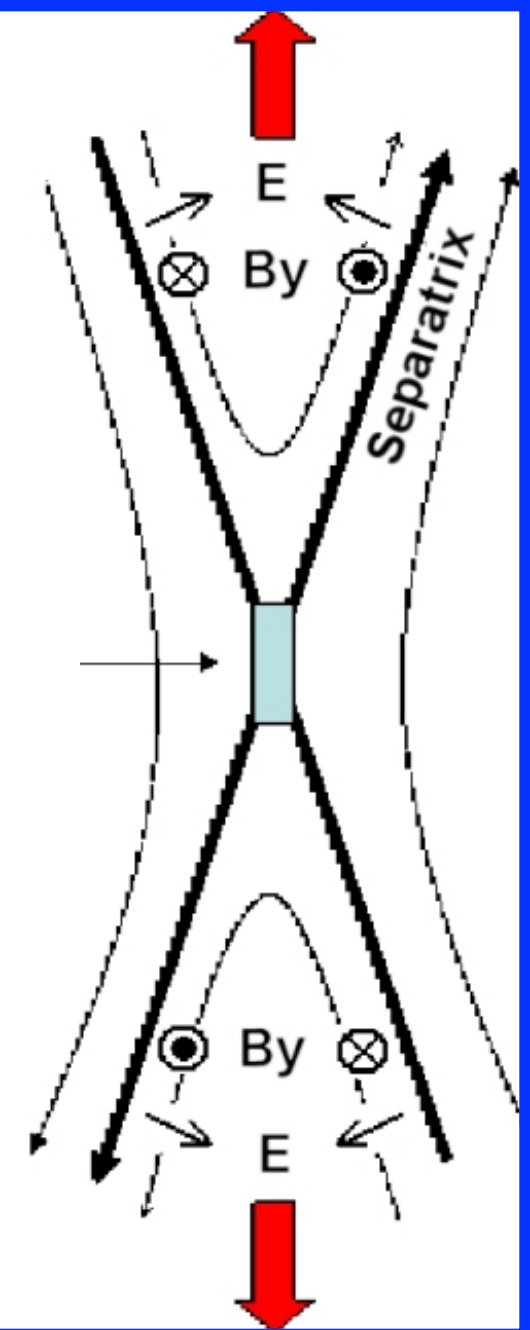
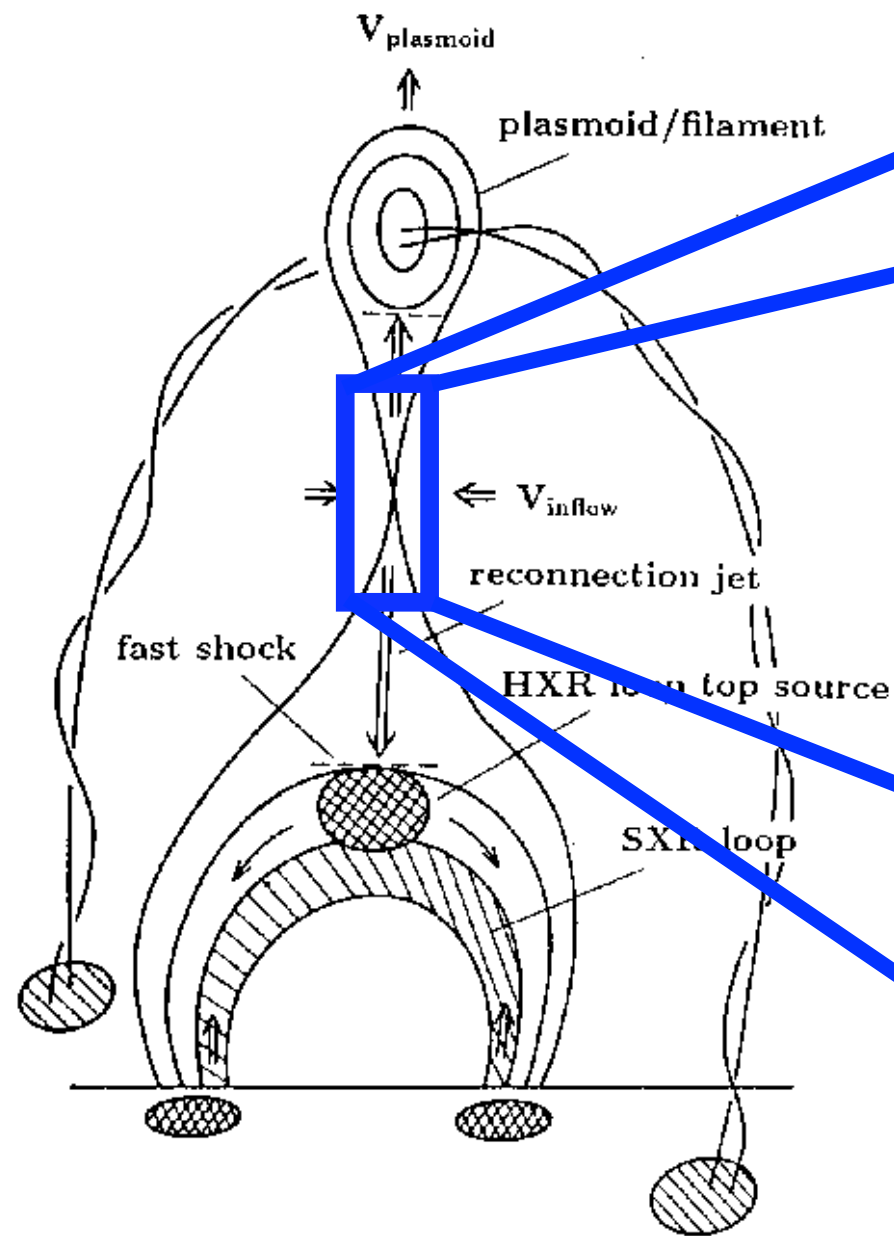
..... Diffusion

The Solar Corona

$$S \sim 10^{14}$$



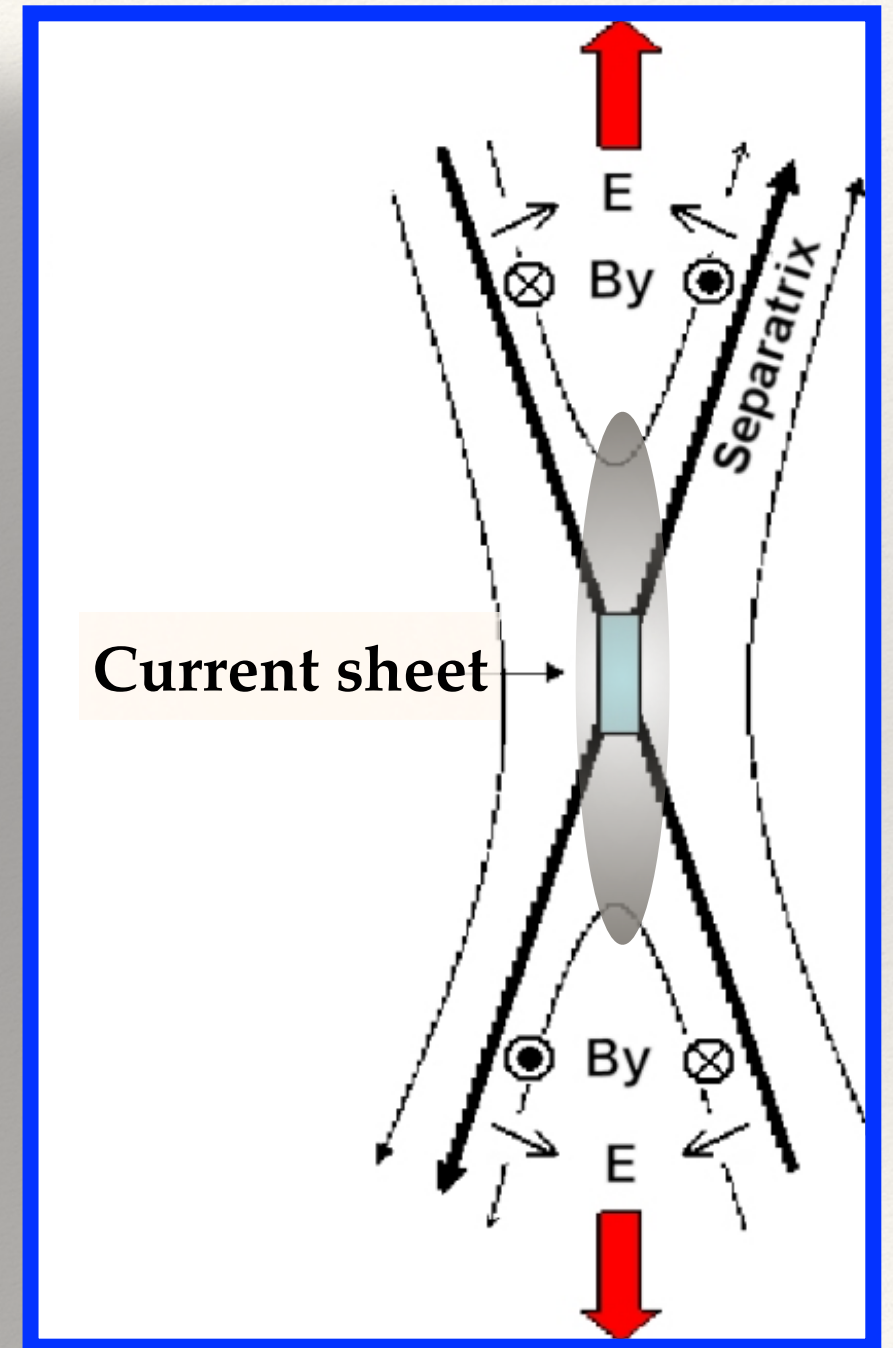
# The “Puzzle” of Magnetic Reconnection (MR)





# The “Puzzle” of Magnetic Reconnection (MR)

- ❖ Large scale MR region:  $\sim 10,000,000$  m.
- ❖ Naively, MR rate very low (years).
- ❖ But: we need high MR rate at flaring sites ( $\sim$ mins or secs)!
- ❖ Three efficient ways:
  1. Assume non-2D (i.e. 3D) geometry! :-)
  2. Make current sheets thin!
  3. Make resistivity high!
- ❖ Howto? Current sheets will fragment until MR rate fits the driving force.
- ❖ What does that mean? We need to describe events:
  - i) on 1000-km spatial, and  $\sim$ hour, time scales
  - ii) ...and on  $\sim$ meter, and  $\sim$ microsecond scales.

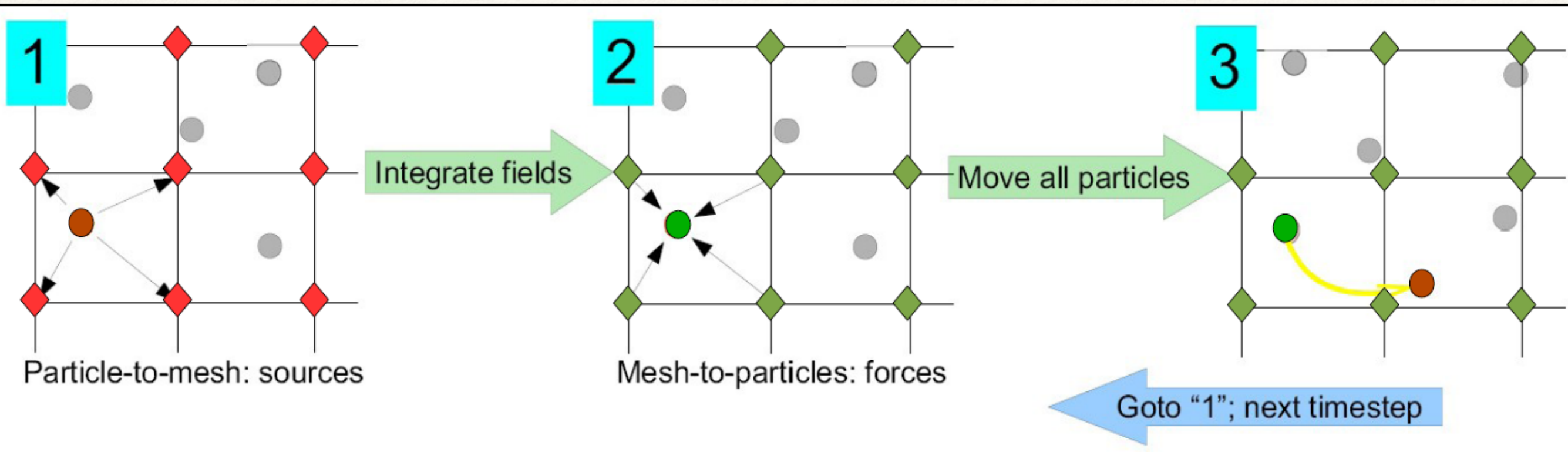




$$\begin{aligned}\nabla \times \frac{1}{\mu_0} \mathbf{B} &= \frac{4\pi}{c} \mathbf{J} + \frac{\epsilon_0}{c} \frac{\partial \mathbf{E}}{\partial t} \\ \nabla \times \mathbf{E} &= -\frac{1}{c} \frac{\partial \mathbf{B}}{\partial t} \\ \nabla \cdot \mathbf{E} &= 4\pi \rho_c / \epsilon_0 \\ \nabla \cdot \mathbf{B} &= 0,\end{aligned}$$

$$\mathbf{F}_L = \frac{\partial \mathbf{p}_s}{\partial t} = \frac{\partial m_{0s} \gamma(v) \mathbf{v}_s}{\partial t} = \frac{q_s}{m_s} (\mathbf{E} + \mathbf{v}_s \times \mathbf{B})$$

$$\frac{\partial f}{\partial t} + \mathbf{p} \cdot \frac{\partial f}{\partial \mathbf{r}} + \frac{q_s}{m_s} (\mathbf{E} + \mathbf{v} \times \mathbf{B}) \cdot \frac{\partial f}{\partial \mathbf{p}} = \left( \frac{\partial f}{\partial t} \right) \Big|_{coll.} = 0$$

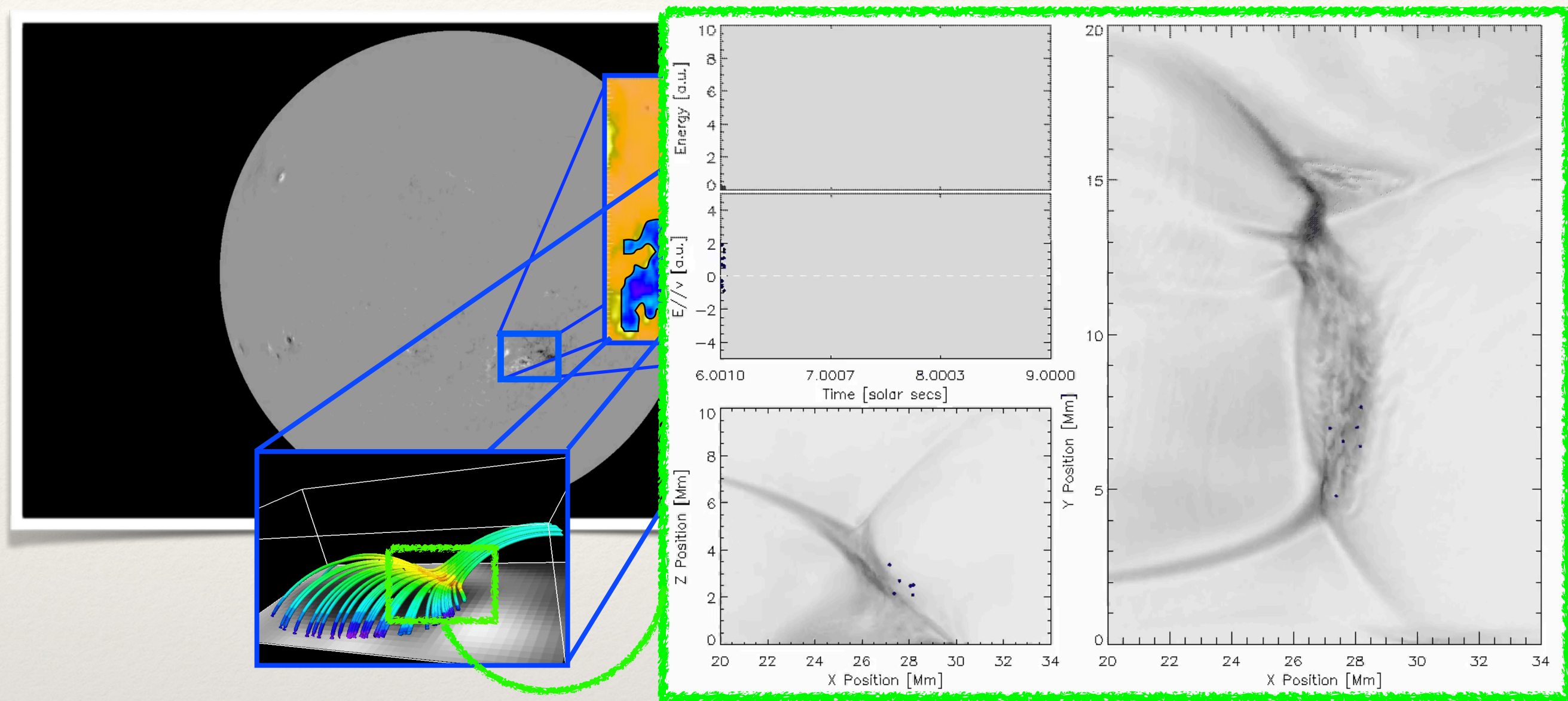


*Particle-In-Cell Codes*

# Kinetic Modeling of Plasmas

- Explicitly integrate EOM for billions of particles
- Construct Maxwell source terms
- Solve Maxwell's equations



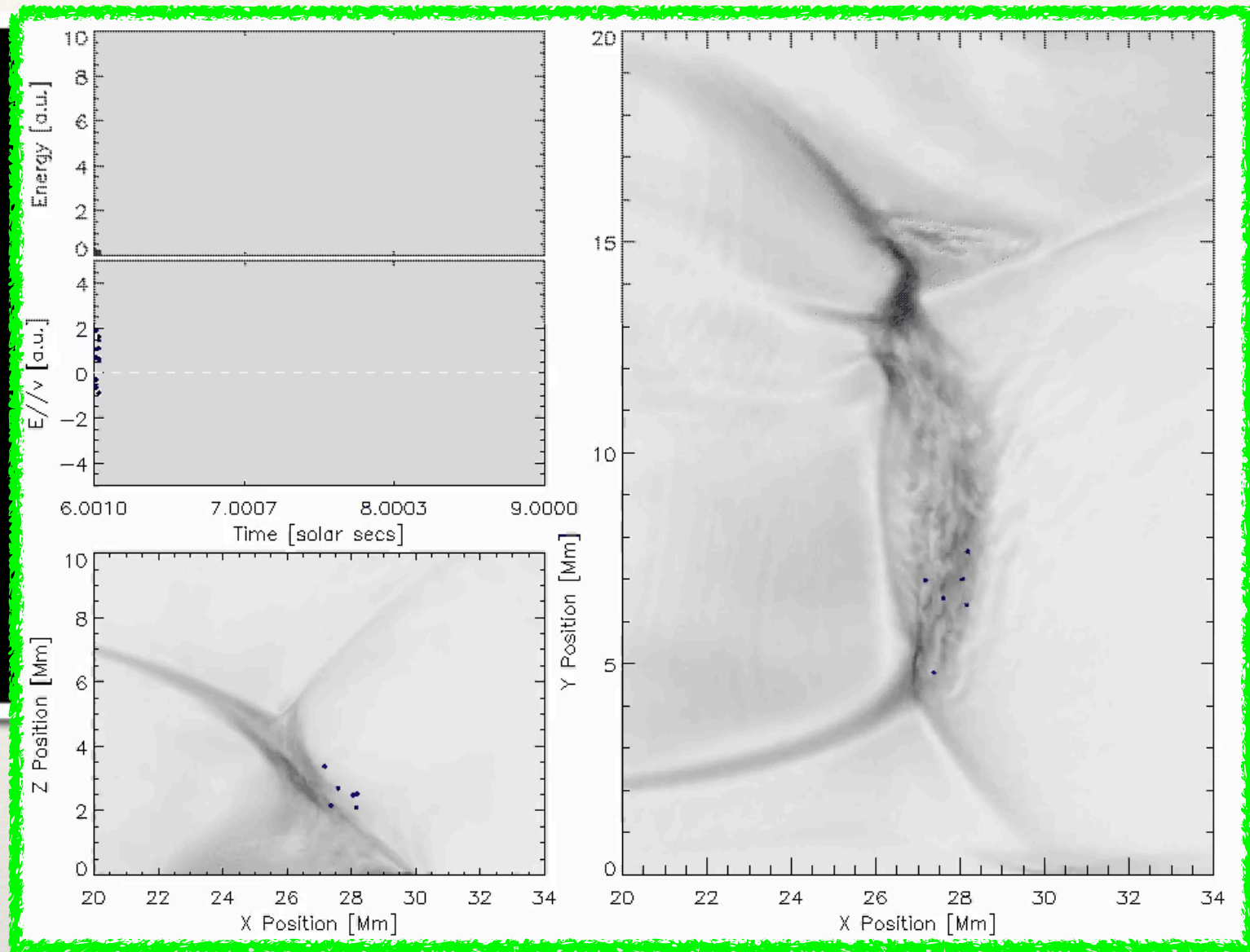
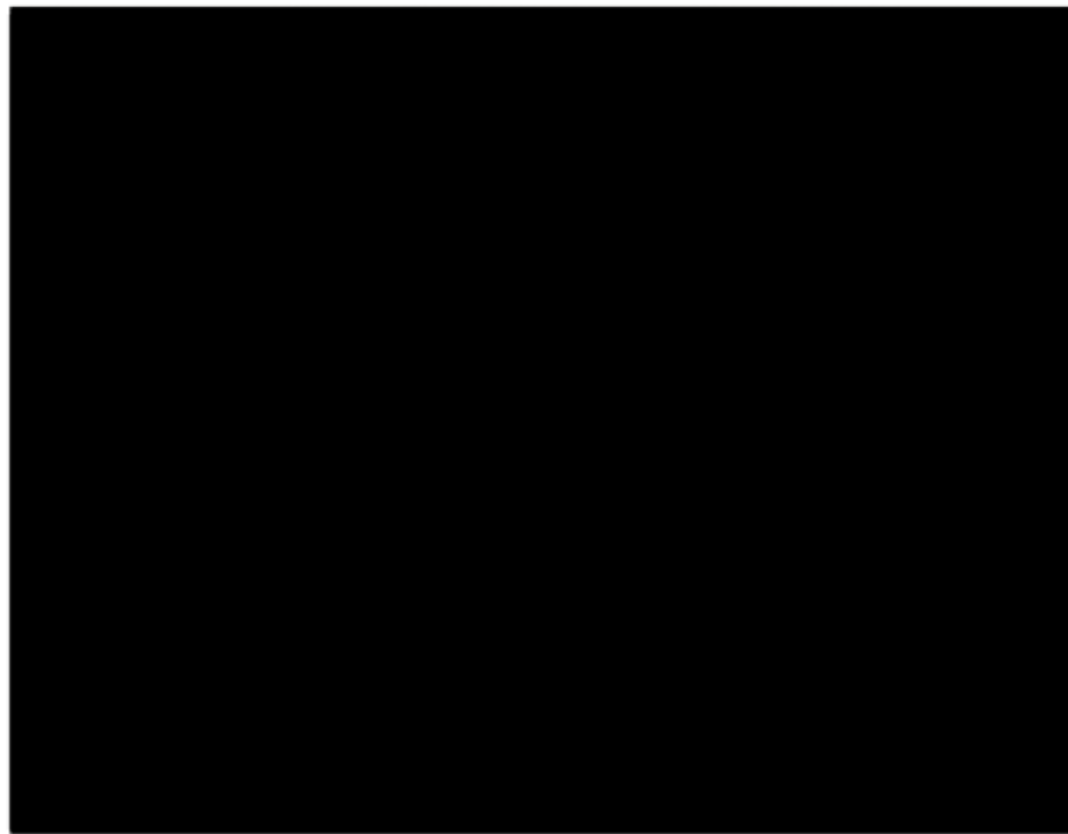


*World's Largest Simulation — 135 billion particles — of kinetics in Solar Flaring Active Region.*

## Computational Modeling of Solar Storms — Today.

- Import magnetic field data from SOHO to MHD code.
- Run MHD code until 'something happens'.
- Port snapshot to fully kinetic code for full dynamics result.





*World's Largest Simulation — 135 billion particles — of kinetics in Solar Flaring Active Region.*

## Computational Modeling of Solar Storms — Today.

- Particles are accelerated
- Mean free paths are system scale
- MHD needed on large scales, but ALSO kinetics on large scales.



- The PIC code should be used globally when looking at highly explosive regions??



*World's Future MHD-KineticPIC Combo Simulation....?*

# Numerical Plasma Physics, Tomorrow?

A successful numerical plasma model seems FORCED to incorporate particle — or PIC — kinetics on large scales, and COMBINE with MHD.

That is the state-of-the-art future.



*The ambitious would go this way*

# Numerical Plasma Physics, Tomorrow?

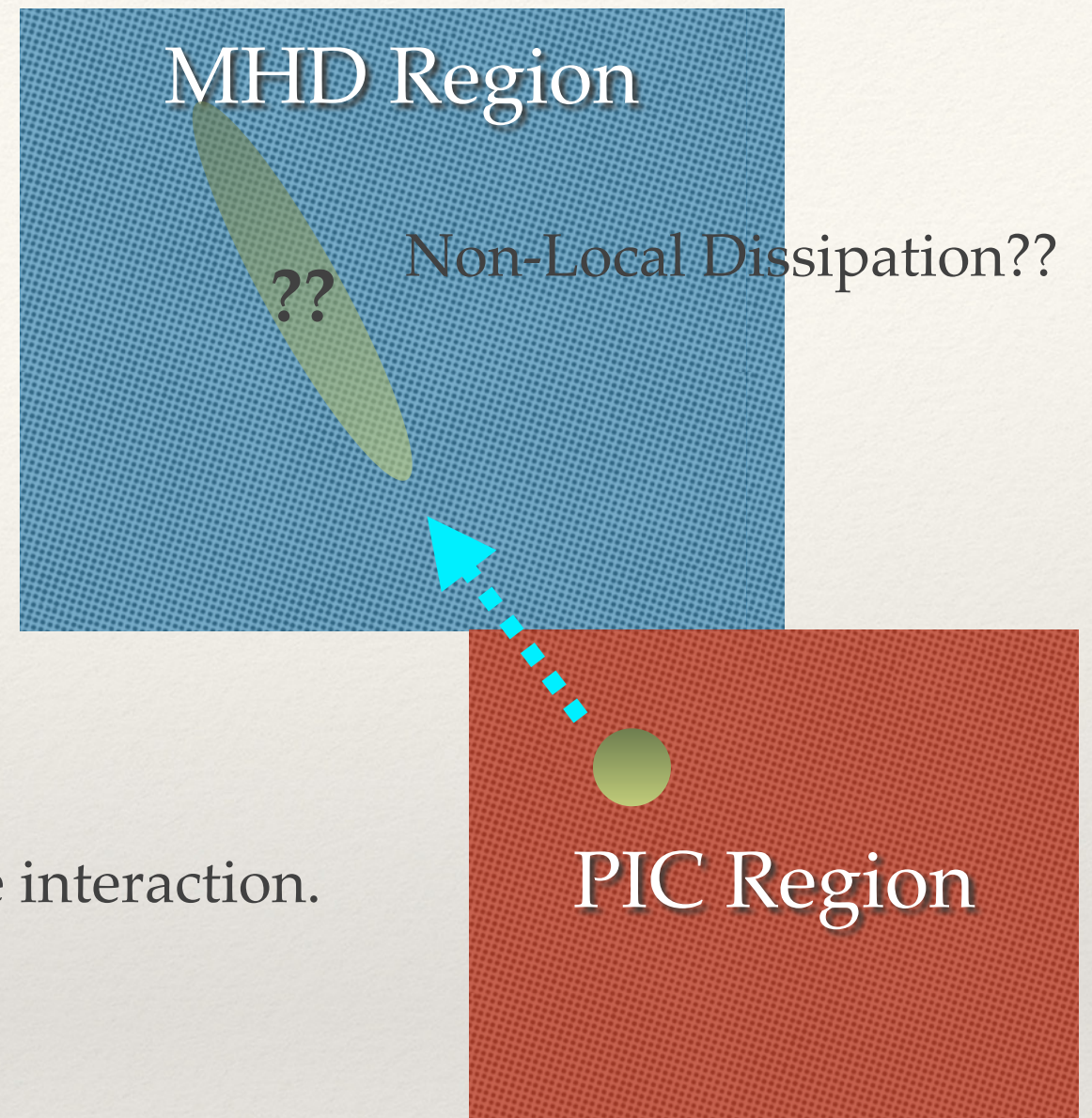
Collision term which incorporates wave-particle interaction.

$$\frac{\partial f^i}{\partial t} + \mathbf{u} \cdot \frac{\partial f^i}{\partial \mathbf{x}} + \frac{q^i}{m^i} (\mathbf{E} + \mathbf{u}_i \times \mathbf{B}) \cdot \frac{\partial f^i}{\partial (\mathbf{u}\gamma)^i} = \left. \frac{\partial f^i}{\partial t} \right|_{coll}$$

Possibly by some Fokker-Planck coupling. Very much “future work”.

$$\frac{\partial p_s}{\partial t} + \vec{v} \cdot \vec{\nabla} p_s + \frac{Z_s e}{m_s} (\vec{E} + \vec{v} \times \vec{B}) \cdot \vec{\nabla}_v p_s = - \frac{\partial}{\partial v_i} (p_s \langle \Delta v_i \rangle) + \frac{1}{2} \frac{\partial^2}{\partial v_i \partial v_j} (p_s \langle \Delta v_i \Delta v_j \rangle) + \left. \frac{\partial f^i}{\partial t} \right|_{coll}$$

⋮  
All other relevant terms





Thank You for Being Here Tonight!